1. We are given a directed graph $G = (V, E)$ on which each edge $(u, v) \in E$ has an associated value $r(u, v)$, which is a real number in the range $0 \leq r(u, v) \leq 1$ that represents the reliability of a communication channel from vertex $u$ to vertex $v$. We interpret $r(u, v)$ as the probability that the channel from $u$ to $v$ will not fail, and we assume these probabilities are independent. Give an efficient algorithm to find the most reliable path between two given vertices.

2. A server has $n$ customers waiting to be served. The service time required by each customer is known in advance: it is $t_i$ minutes for customer $i$. So if, for example, the customers are served in order of increasing $i$, then the $i$th customer has to wait $\sum_{j=1}^{i} t_j$ minutes.

We wish to minimize the total waiting time

$$T = \sum_{i=1}^{n} (\text{time spent waiting by customer } i).$$

Describe an efficient algorithm for computing the optimal order in which to process the customers and give a brief justification of its running time and correctness.