# Natural Language Processing CSCI 4152/6509 - Lecture 10 Introduction to Probabilistic NLP 

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## Previous Lectures

- Discussion about evaluation methods for classifiers
- Similarity-based Text Classification
- CNG classification method
- Edit distance:
- introduction, properties, dynamic programming approach, example, algorithm


## Edit Distance Example (to finish)

- distance between 'there' and 'ythre'


## Part III: Probabilistic Approach to NLP <br> Logical versus Plausible Reasoning

- As a part of AI (Artificial Intelligence), NLP follows two main approaches to computer reasoning, or computer inference:

1. logical reasoning

- known also as classical, symbolic, knowledge-based AI
- monotonic: once conclusion drawn, never retracted
- certain: conclusions certain, given assumptions

2. plausible reasoning

- examples: probabilistic, fuzzy logic, neural networks
- non-monotonic
- uncertain


## Plausible Reasoning

- How to combine ambiguous, incomplete, and contradicting evidence to draw reasonable conclusions?
- Typical approach: make plausible inference of some hidden structure from observations
- Examples:

| Observations (input) |  | Hidden Structure (output) |
| :---: | :--- | :---: |
| symptoms | $\rightarrow$ | illness |
| pixel matrix | $\rightarrow$ | object, relations |
| speech signal | $\rightarrow$ | phonemes, words |
| word sequence | $\rightarrow$ | meaning |
| sentence | $\rightarrow$ | parse tree |
| word sequence | $\rightarrow$ | POS tags, names, entities |
| words in e-mail Subject: | $\rightarrow$ | Is message spam? Yes/No |
| text | $\rightarrow$ | text category (class) |

## Probabilistic NLP as a Plausible Reasoning Approach

- Regular expressions and finite automata are example of logical or knowledge-based approach to NLP
- Plausible approaches to NLP:

1. Probabilistic: use of Theory of Probability, also known as stochastic or statistical NLP

- Alternative plausible approaches, examples:

2. neural networks,
3. kernel methods,
4. fuzzy logic, fuzzy sets,
5. Dempster-Shafer theory
6. rough sets,
7. default logic, ...

## Review of Basics of Probability Theory

- You should have this background from previous courses; this is just a review,
- discussed a bit in the textbook: [JM] 5.5, and [MS] 2.1
- Simple event or basic outcome
- e.g., rolling a die, choosing a letter
- Event space: the set of all outcomes, usually denoted $\Omega$
- Event or outcome is a set of simple events or basic outcomes
- In other words event is any subset of $\Omega$; i.e., $A \subseteq \Omega$
- Each event is associated with a probability, which is a number between 0 and 1, inclusive: $0 \leq \mathrm{P}(A) \leq 1$


## Probability Examples

- $\mathrm{P}($ "rolling a 6 with a die" $)=1 / 6$
- Choosing a letter of English alphabet:
- If we choose uniformly: $\mathrm{P}\left({ }^{\prime} \mathrm{a}^{\prime}\right)=1 / 26 \approx 0.04$
- Choosing from a text: $\mathrm{P}\left({ }^{\prime} \mathrm{a}\right.$ ' $) \approx 0.08$
- Remember our output from "Tom Sawyer":

356970.1204 e<br>288970.0974 t<br>235280.0793 a<br>232640.0784 о<br>202000.0681 n

## Probability Axioms

- (Nonnegativity) $\mathrm{P}(A) \geq 0$, for any event $A$
- (Additivity) for disjoint events $A$ and $B$, i.e., if $A, B \subset \Omega$ and $A \cap B=\emptyset$, then
$\mathrm{P}(A \cup B)=\mathrm{P}(A)+\mathrm{P}(B)$
or, more generally,
$\mathrm{P}\left(A_{1} \cup A_{2} \cup \ldots\right)=\mathrm{P}\left(A_{1}\right)+\mathrm{P}\left(A_{2}\right)+\ldots$
- (Normalization) $\mathrm{P}(\Omega)=1$, where $\Omega$ is the entire sample space.
- Some consequences of the above axioms are: $\mathrm{P}(\emptyset)=0$ and $\mathrm{P}(\Omega-A)=1-\mathrm{P}(A)$


## Independent and Dependent Events

- Independent events $A$ and $B$ (definition):

$$
\mathrm{P}(A, B)=\mathrm{P}(A) \cdot \mathrm{P}(B)
$$

- Use of comma in: $\mathrm{P}(A, B)=\mathrm{P}(A \cap B)$
- Example: choosing two letters in text
(1) Choosing independently:

$$
\mathrm{P}\left({ }^{\prime} \mathrm{t}^{\prime}\right)=0.1, \mathrm{P}\left(\mathrm{'h}^{\prime}\right)=0.07, \mathrm{P}\left(\mathrm{'t}^{\prime},{ }^{\prime} \mathrm{h} \text { ' }\right)=0.007
$$

(2) Choosing two consecutive letters (dependent events): $\mathrm{P}\left({ }^{\prime} \mathrm{t}\right.$ ', 'h') $=0.04$

## Conditional Probability

- Conditional probability

$$
\mathrm{P}(A \mid B)=\frac{\mathrm{P}(A, B)}{\mathrm{P}(B)}
$$

- Expressing independency using conditional probability Two events $A$ are $B$ are independent if and only if:

$$
\mathrm{P}(A \mid B)=\mathrm{P}(A)
$$

This is an alternative definition of independent events.

## Annotation with More Events

- There is a bit of flexibility in using notation; e.g.,
- $\mathrm{P}(A, B, C)=\mathrm{P}(A \cap B \cap C)$
- $\mathrm{P}(A \mid B, C)=\mathrm{P}(A \mid B \cap C)$
- $\mathrm{P}(A, B, C \mid D, E, F)=\mathrm{P}(A \cap B \cap C \mid D \cap E \cap F)$
- and so on.
- Three independent events: $\mathrm{P}(A, B, C)=\mathrm{P}(A) \mathrm{P}(B) \mathrm{P}(C)$
- Conditionally independent events

$$
\mathrm{P}(A, B \mid C)=\mathrm{P}(A \mid C) \cdot \mathrm{P}(B \mid C)
$$

## Bayes' Theorem

- Bayes' theorem (one form):

$$
\mathrm{P}(A \mid B)=\frac{\mathrm{P}(B \mid A) \cdot \mathrm{P}(A)}{\mathrm{P}(B)}
$$

- The second form is based on breaking the set $B$ into disjoint sets $B=A_{1} \cup A_{2} \cup \ldots$ :

$$
\mathrm{P}\left(A_{i} \mid B\right)=\frac{\mathrm{P}\left(B \mid A_{i}\right) \cdot \mathrm{P}\left(A_{i}\right)}{\mathrm{P}(B)}=\frac{\mathrm{P}\left(B \mid A_{i}\right) \cdot \mathrm{P}\left(A_{i}\right)}{\sum_{i} \mathrm{P}\left(B \mid A_{i}\right) \mathrm{P}\left(A_{i}\right)}
$$

## Bayesian Inference and Generative Models

- We will use Bayesian Inference on Generative Models
- Generative Models, also known as Forward Generative Models
- One way of representing knowledge with a probabilistic model



## Notation Remark: max and argmax

- max is the maximum value of a function
- $\arg \max$ is an argument value for which function achieves the maximum



## Bayesian Inference: Using Bayes' Theorem

- Bayesian inference is a principle of combining evidence

$$
\begin{aligned}
\text { conclusion } & =\underset{\text { possible truth }}{\arg \max } P(\text { possible truth } \mid \text { evidence }) \\
& =\underset{\text { possible truth }}{\arg \max } \frac{P(\text { evidence } \mid \text { possible truth }) P(\text { possible truth })}{P(\text { evidence })} \\
& =\underset{\text { possible truth }}{\arg \max } P(\text { evidence } \mid \text { possible truth }) P(\text { possible truth })
\end{aligned}
$$

- application to speech recognition: acoustic model and language model


## Bayesian Inference: Speech Recognition Example

- evidence $\rightarrow$ sound
- possible truth $\rightarrow$ utterance (words spoken)
- our best guess about utterance $\rightarrow$ utterance*

$$
\begin{aligned}
\text { utterance }^{*} & =\underset{\text { all utterances }}{\arg \max } P(\text { utterance } \mid \text { sound }) \\
& =\underset{\text { all utterances }}{\arg \max } \frac{P(\text { sound } \mid \text { utterance }) P(\text { utterance })}{P(\text { sound })} \\
& =\underset{\text { utterance }}{\arg \max } P(\text { sound } \mid \text { utterance }) P(\text { utterance })
\end{aligned}
$$

