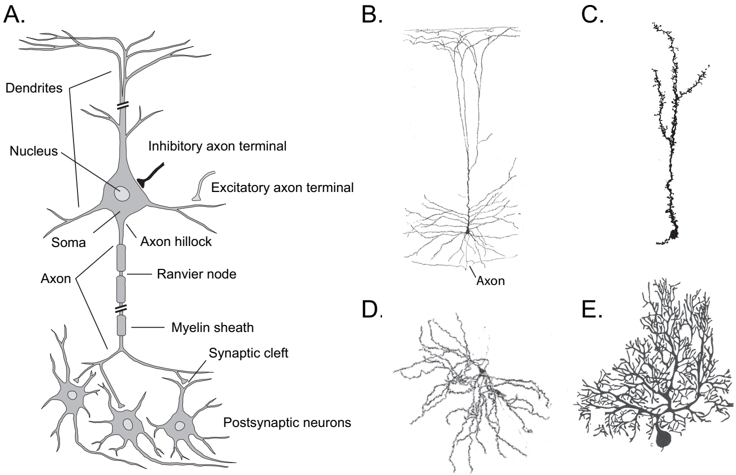
Fundamentals of Computational Neuroscience 2e

Thomas Trappenberg

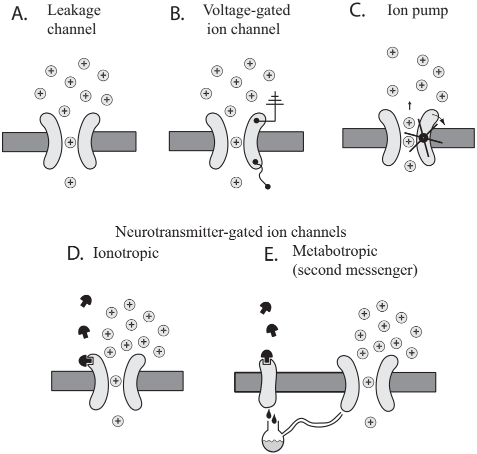
January 16, 2009

Chapter 2: Neurons and conductance-based model

Biological background

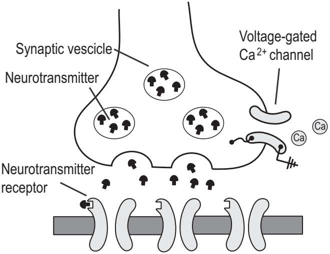


Ion channels

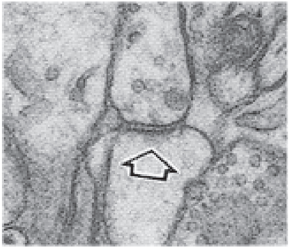


Synapse

A. Schematic synapse



B. Microscope image of synapse



non-NMDA: GABA, AMPA

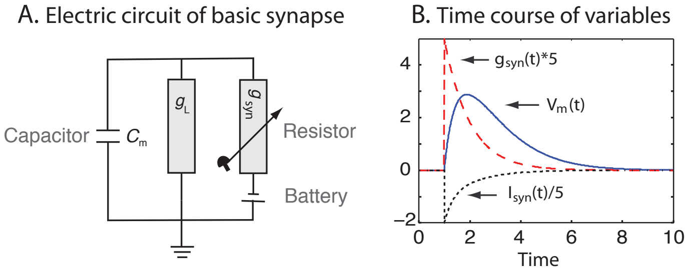
$$\Delta V_{\mathrm{m}}^{\mathrm{non-NMDA}} \propto t \, \mathrm{e}^{-t/t^{\mathrm{peak}}}$$

Conductance-based models

$$c_m \frac{\mathrm{d}V(t)}{dt} = -I \tag{1}$$

$$I(t) = g_0 V(t) - g(t)(V(t) - E_{\mathrm{syn}}) \tag{2}$$

$$\tau_{\mathrm{syn}} \frac{\mathrm{d}g(t)}{\mathrm{d}t} = -g(t) + \delta(t - t_{\mathrm{pre}} - t_{\mathrm{delay}}) \tag{3}$$



MATLAB Program

```
%% Synaptic conductance model to simulate an EPSP
 clear; clf; hold on;

%% Setting some constants and initial values
 c_m=1; g_L=1; tau_syn=1; E_syn=10; delta_t=0.01;
 g_syn(1)=0; I_syn(1)=0; v_m(1)=0; t(1)=0;

%% Numerical integration using Euler scheme
 for step=2:10/delta_t
   t(step)=t(step-1)+delta_t;
   if abs(t(step)-1)<0.001; g_syn(step-1)=1; end
   g_syn(step)= (1-delta_t/tau_syn) * g_syn(step-1);
   I_syn(step)= g_syn(step) * (v_m(step-1)-E_syn);
   v_m(step) = (1-delta_t/c_m*g_L) * v_m(step-1) ...
                   - delta_t/c_m * I_syn(step);
 end

%% Plotting results
 plot(t,v_m); plot(t,g_syn*5,'r--'); plot(t,I_syn/5,'k:')
```

Hodgkin–Huxley model

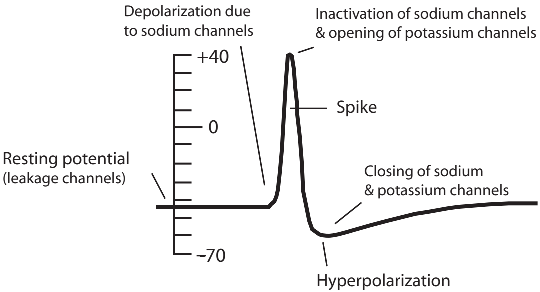
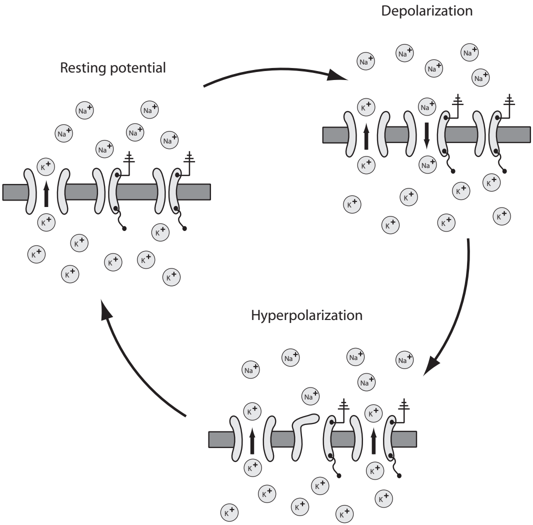


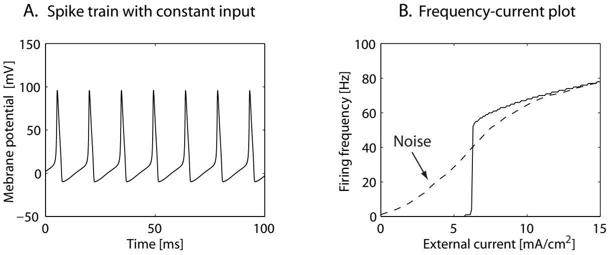
Figure: Typical form of an action potential; redrawn from an oscilloscope picture from Hodgkin and Huxley (1939).

The minimal mechanisms

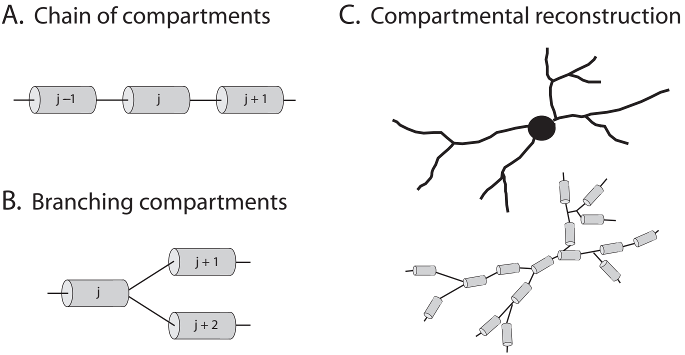


Hodgkin–Huxley equations and simulation

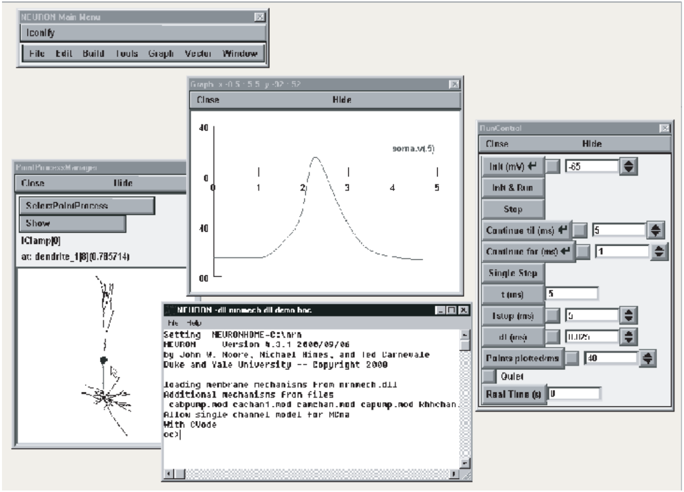
$$
\begin{aligned}
C\frac{\mathrm{d}V}{\mathrm{d}t} &= -g_{\mathrm{K}}n^4(V-E_{\mathrm{K}}) - g_{\mathrm{Na}}m^3h(V-E_{\mathrm{Na}}) - g_{\mathrm{L}}(V-E_{\mathrm{L}}) + I(t) \\
\tau_{\mathrm{n}}(V)\frac{\mathrm{d}n}{\mathrm{d}t} &= -[n-n_0(V)] \\
\tau_{\mathrm{m}}(V)\frac{\mathrm{d}m}{\mathrm{d}t} &= -[m-m_0(V)] \\
\tau_{\mathrm{h}}(V)\frac{\mathrm{d}h}{\mathrm{d}t} &= -[h-h_0(V)]
\end{aligned}
$$



Compartmental models



Simulators



NEURON Main Menu
Iconify
File Edit Build Tools Graph Vector Window
Close Hide
soma.v(.5)
SelectPointProcess
Show
IClamp[0]
at: dendrite_1[8](0.785714)
RunControl
Init (mV)
-65
Init & Run
Stop
Continue til (ms)
Continue for (ms)
Single Step
t (ms)
Tstop (ms)
dt (ms)
Points plotted/ms
40
Quiet
Real Time (s)
Setting NEURONHOME=C:\nrn
NEURON -- Version 4.3.1 2000/09/06
by John W. Moore, Michael Hines, and Ted Carnevale
Duke and Yale University -- Copyright 2000
loading membrane mechanisms from nrnmech.dll
Additional mechanisms from files
cabpump.mod cachan1.mod camchan.mod capump.mod khhchan.
Allow single channel model for MCna
With CVode
oc>

Further Readings

Mark F. Bear, Barry W. Connors, and Michael A. Paradiso (2006), **Neuroscience: exploring the brain**, Lippincott Williams & Wilkins , 3rd edition.

Eric R. Kandel, James H. Schwartz, and Thomas M. Jessell (2000), **Principles of neural science**, McGraw-Hill, 4th edition

Gordon M. Shepherd (1994), **Neurobiology**, Oxford University Press, 3rd edition.

Christof Koch (1999), **Biophysics of computation; information processing in single neurons**, Oxford University Press

Christof Koch and Idan Segev (eds.) (1998), **Methods in neural modelling**, MIT Press, 2nd edition.

C. T. Tuckwell (1988), **Introduction to theoretical neurobiology**, Cambridge University Press.

Hugh R. Wilson (1999) **Spikes, decisions and actions: dynamical foundations of neuroscience**, Oxford University Press. See also his paper in J. Theor. Biol. 200: 375–88, 1999.