

# Dynamic and Heterogeneous Ensembles for Time Series Forecasting

Vítor Cerqueira<sup>1</sup>, Luís Torgo<sup>1</sup>, Mariana Oliveira<sup>1</sup>, and Bernhard Pfahringer<sup>2</sup>

INESCTEC / University of Porto, Portugal<sup>1</sup>

University of Auckland, New Zealand<sup>2</sup>

## Objectives

The main goal of this work is to uncover new techniques for adaptively combining diverse base learners of an ensemble model for univariate time series forecasting.

## Motivation and assumptions

- Different learning models have different areas of expertise across the input space  $\Rightarrow$  **ensemble heterogeneity**;
- Recurring structures are common and forecasting models have varying relative performance over time  $\Rightarrow$  **dynamic combination**.

## Forecasting $t+1$

Each base model  $M_j, \forall j \in \{1, \dots, m\}$  is built to approximate a function  $Y_{t+1} = f(Y_t, \dots, Y_{t-K})$  using the available time series  $Y$ .

Weighting predictions according to recent performance:

- The MSE of each forecaster is tracked over the last  $\Omega$  observations;
- The forecaster's weight is computed by applying the complementary Gaussian error function, **erfc**, to the MSE.

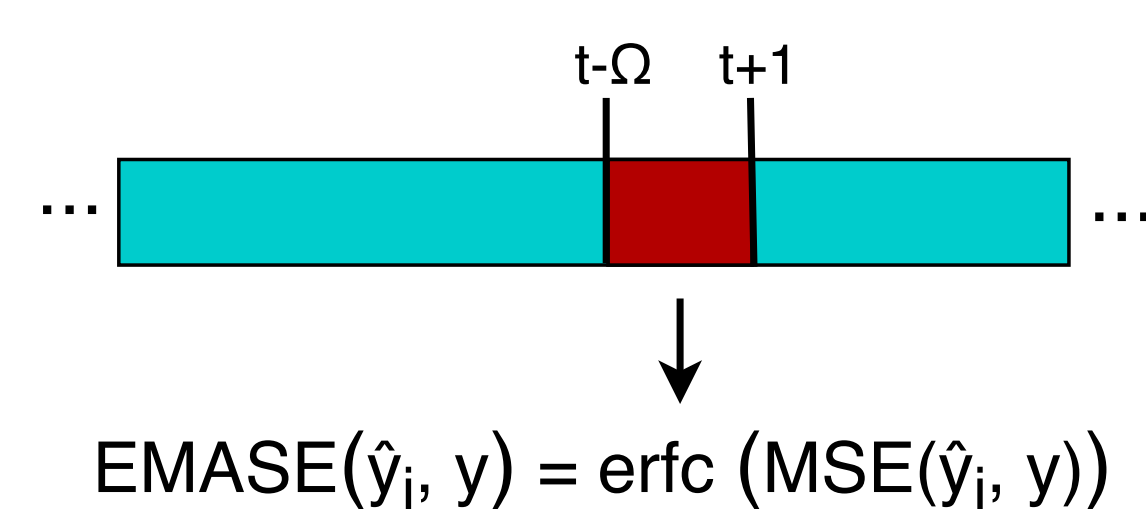


Figure 1: Computing EMASE – Erfc Moving Average Squared Error

Suspending models with poor recent performance:

- The ensemble has a dynamic composition – at each point, the top  $\alpha\%$  of models in the last  $\Omega$  observations are weighted.

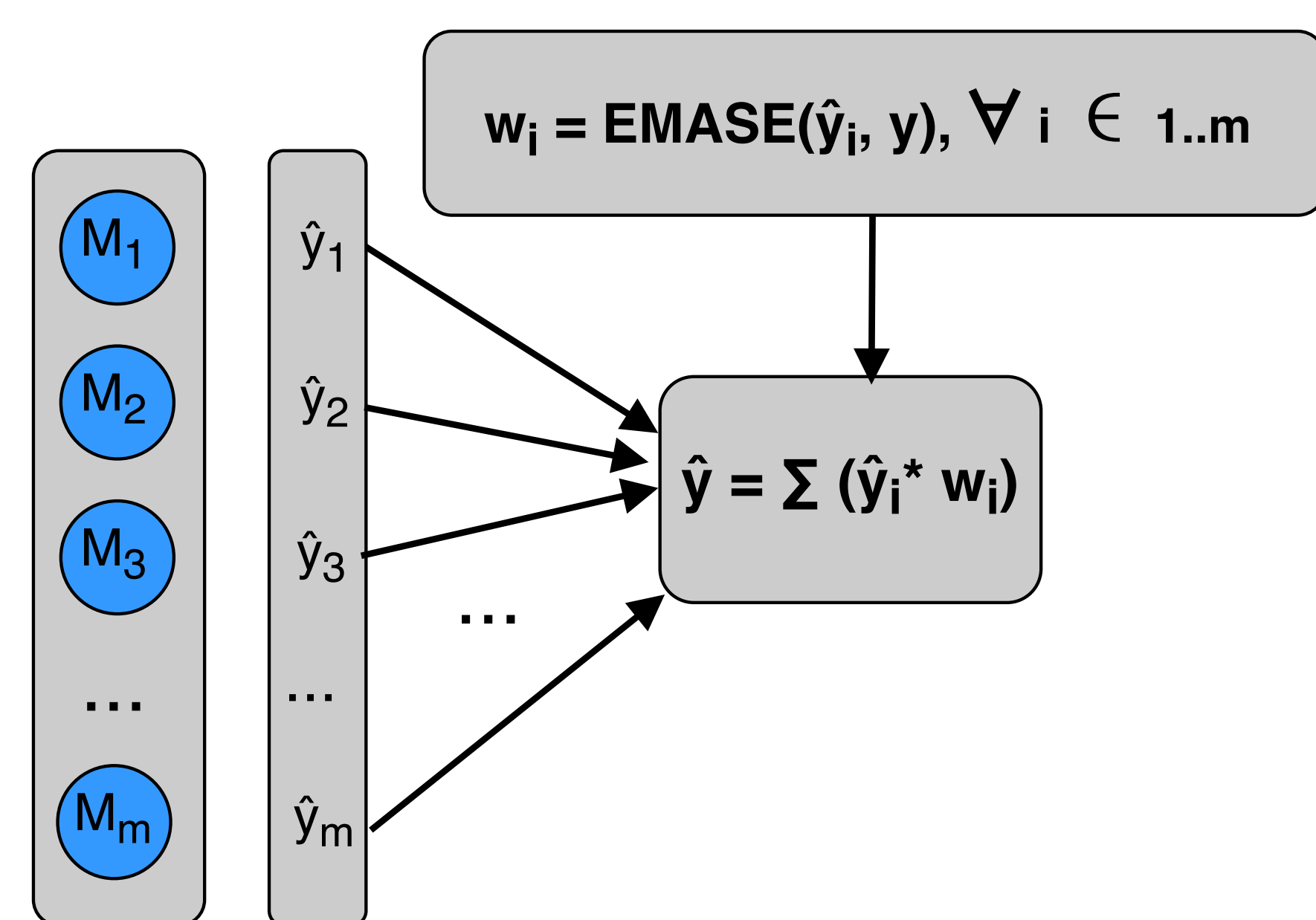


Figure 2: The prediction of each forecaster,  $\hat{y}_i$  is weighted according to EMASE.

## Acknowledgements

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## Encouraging data diversity

$$Y_{[N,K]} = \begin{bmatrix} y_1 & y_2 & \dots & y_{K-1} & y_K \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ y_{i-K+1} & y_{i-K+2} & \dots & y_{i-1} & y_i \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ y_{N-K+1} & y_{N-K+2} & \dots & y_{N-1} & y_N \end{bmatrix}$$

Subsetting embedding size (columns) and training window (rows)

- embedding size diversity:  $\mathbf{K}, \mathbf{K}/2, \mathbf{K}/4$
- training window diversity:  $\mathbf{N}, \mathbf{N}/2, \mathbf{N}/4$ 
  - Leading to 9 different data combinations available for training

## Empirical Results

- Base models include SVR; Multi-layer perceptron; Gaussian Processes; Linear regression; Random Forest; Generalized Boosted regression; PPR; MARS, and Rule-based regression
- 10% of the models with top performance in the last 50 observations are weighted for predicting  $t+1$ ;
- Testing on 16 time series from several domains

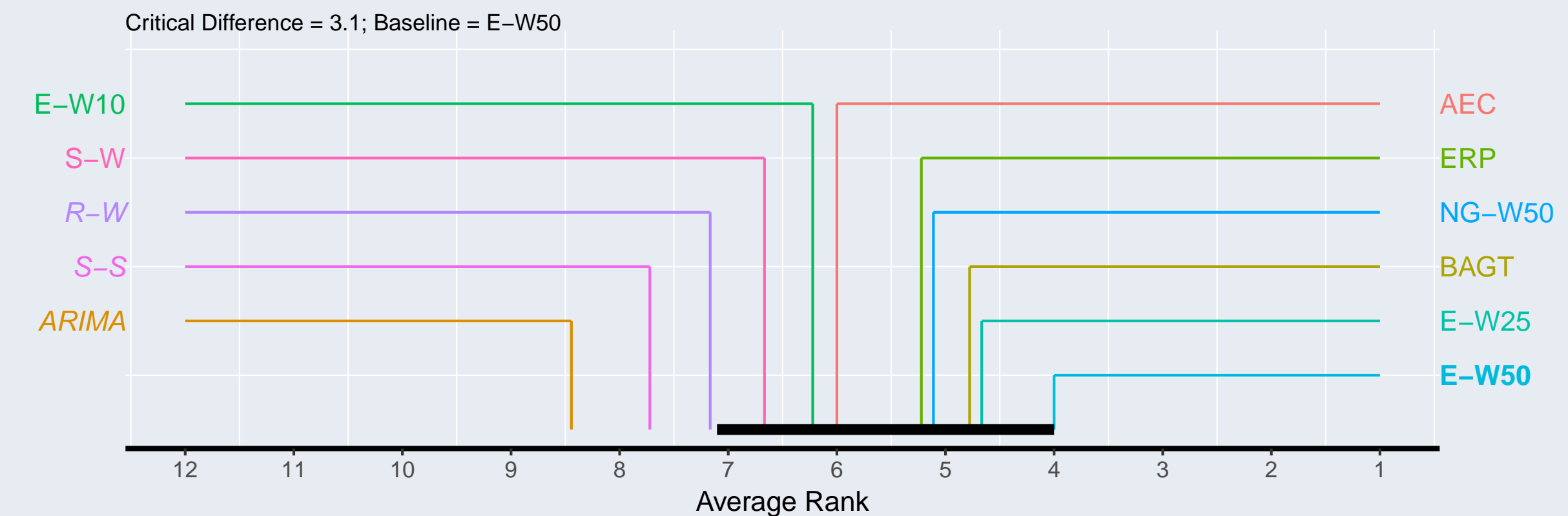


Figure 3: Comparing the proposed method **E-W50** to baselines & state of the art with a post-hoc Bonferroni-Dunn test. **NG-W50** is the state-of-art windowing combination approaches; **BAGT** is a bagging of trees specially designed for time series forecasting; **S-W** weights forecasters according to error in the training set; **S-S** combines models using a simple average; and **ERP**, **R-W**, and **AEC** are other dynamic combination approaches in the literature.

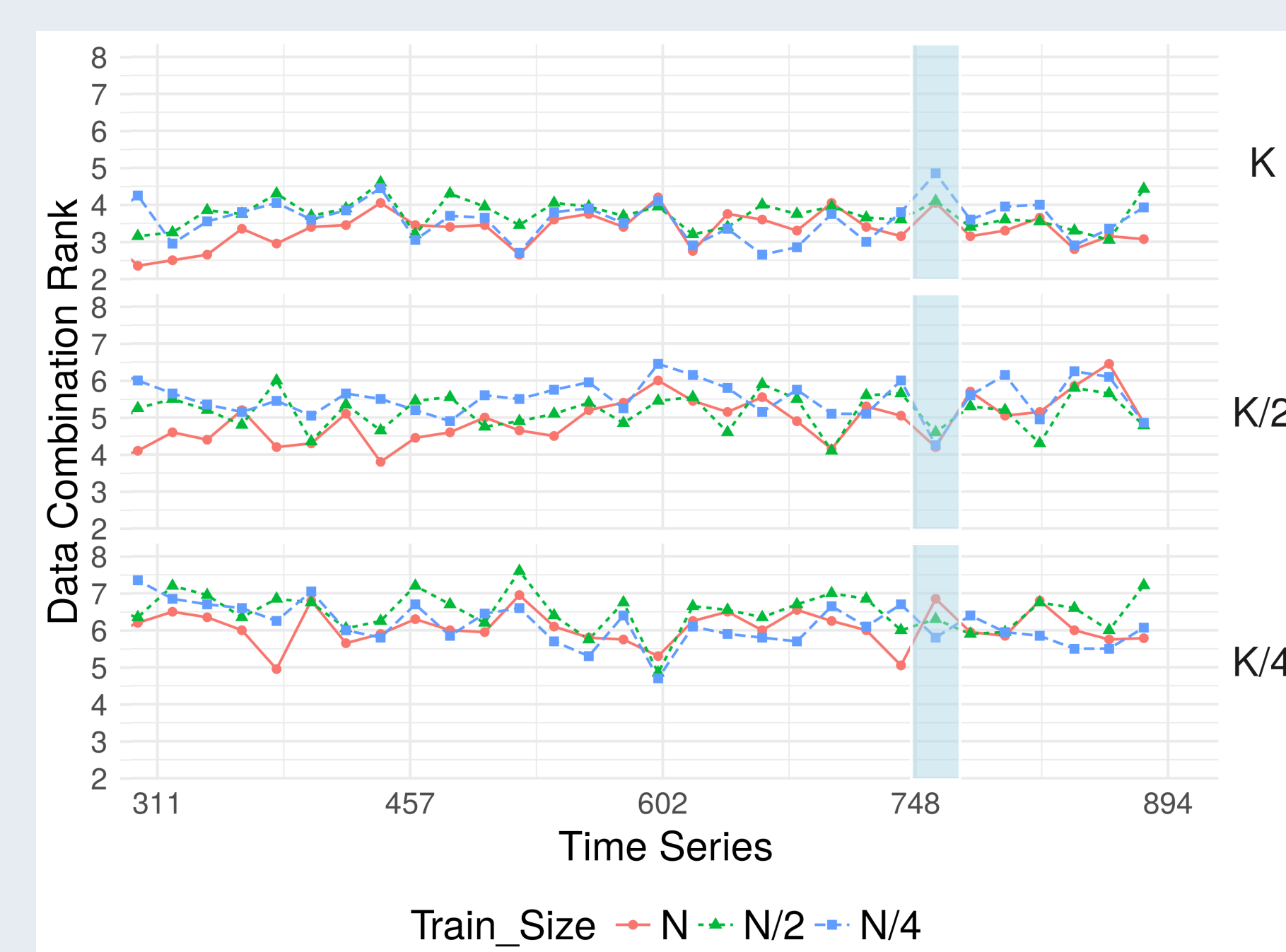


Figure 4: Squared error rank of each data combination strategy. There is systematic evidence that subsets of the original time series show better performance in some time series intervals.