

Predictive Analytics

Solutions to Hands On Exercises

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Hands on LDAs - the Vehicle data set

The data set `Vehicle` is available in package **mlbench**. Load it and explore its help page to grab a minimal understanding of the data and then answer the following questions:

- 1 Obtain a random split of the data into two sub-sets using the proportion 80%-20%. [solution](#)
- 2 Obtain a linear discriminant using the larger set. [solution](#)
- 3 Obtain the predictions of the obtained model on the smaller set. [solution](#)
- 4 Obtain a confusion matrix of the predictions and calculate the respective accuracy. [solution](#)

Solutions to Exercise 1

- Obtain a random split of the data into two sub-sets using the proportion 80%-20%. [solution](#)

```
data(Vehicle, package="mlbench")
idx.tr <- sample(1:nrow(Vehicle), as.integer(0.8*nrow(Vehicle)))
tr <- Vehicle[idx.tr,]
ts <- Vehicle[-idx.tr,]
```

[Go Back](#)

Solutions to Exercise 2

- Obtain a linear discriminant using the larger set.

```
library(MASS)
model <- lda(Class ~ ., tr)
```

[Go Back](#)

Solutions to Exercise 3

- Obtain the predictions of the obtained model on the smaller set.

```
preds <- predict(model, ts)
```

[Go Back](#)

Solutions to Exercise 4

- Obtain a confusion matrix of the predictions and calculate the respective accuracy.

```
cm <- table(preds$class, ts$Class)
acc <- sum(diag(cm)) / sum(cm)
cat("The accuracy is ", round(acc*100, 2), "%.\n")

## The accuracy is 30 %.
```

Hands on Linear Regression - the Boston data set

The data set `Boston` is available in package **MASS**. Load it and explore its help page to grab a minimal understanding of the data and then answer the following questions:

- 1 Obtain a random split of the data into two sub-sets using the proportion 70%-30%. [solution](#)
- 2 Obtain a multiple linear regression model using the larger set. [solution](#)
- 3 Check the diagnostic information provided for the model. [solution](#)
- 4 Obtain the predictions of the obtained model on the smaller set. [solution](#)
- 5 Obtain the mean squared error of these predictions and also an error scatter plot. [solution](#)

Solutions to Exercise 1

- Obtain a random split of the data into two sub-sets using the proportion 70%-30%. [solution](#)

```
data(Boston, package="MASS")
idx.tr <- sample(1:nrow(Boston), as.integer(0.7*nrow(Boston))
tr <- Boston[idx.tr,]
ts <- Boston[-idx.tr,]
```

[Go Back](#)

Solutions to Exercise 2

- Obtain a multiple linear regression model using the larger set.

```
model <- lm(medv ~ ., tr)
```

[Go Back](#)

Solutions to Exercise 3

- Check the diagnostic information provided for the model.

```
summary(model)

##
## Call:
## lm(formula = medv ~ ., data = tr)
##
## Residuals:
##     Min      1Q  Median      3Q     Max 
## -10.776 -2.371 -0.664  1.906 25.349 
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)    
## (Intercept) 2.53e+01  5.93e+00   4.27  2.6e-05 ***
## crim        -6.74e-02 3.91e-02  -1.73  0.08534 .  
## zn          4.96e-02  1.50e-02   3.29  0.00109 ** 
## indus       5.14e-04  6.43e-02   0.01  0.99364    
## chas        3.28e+00  9.18e-01   3.57  0.00041 *** 
## nox         -1.09e+01 4.07e+00  -2.67  0.00793 ** 
## rm          4.71e+00  4.96e-01   9.50 < 2e-16 ***
## age         -3.91e-02 1.45e-02  -2.69  0.00749 ** 
## dis         -1.60e+00 2.22e-01  -7.18  4.4e-12 ***
## rad          2.38e-01  7.48e-02   3.18  0.00162 ** 
## tax         -1.34e-02 4.15e-03  -3.22  0.00140 ** 
## ptratio     -8.23e-01 1.40e-01  -5.89  9.4e-09 *** 
## black       1.39e-02  3.19e-03   4.34  1.9e-05 *** 
## lstat      -3.93e-01  5.46e-02  -7.19  4.1e-12 *** 
## ---
```

Solutions to Exercise 4

- Obtain the predictions of the obtained model on the smaller set.

```
preds <- predict(model, ts)
```

[Go Back](#)

Solutions to Exercise 5

- Obtain the mean squared error of these predictions and also an error scatter plot.

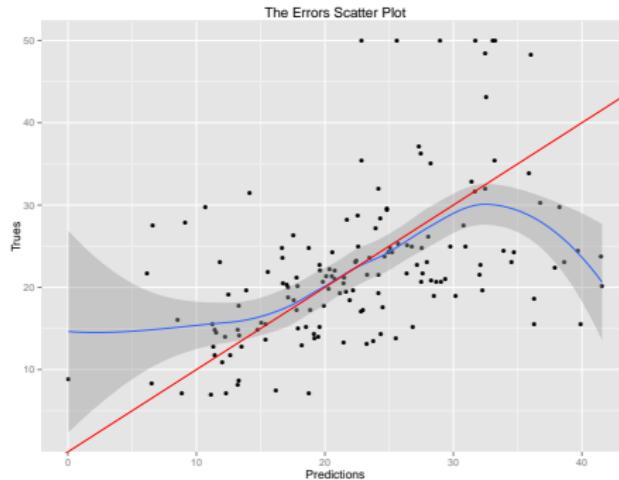
```
mse <- mean((preds-ts$medv)^2)
cat("The mean squared error is ", round(mse*100, 2), "\n")

## The mean squared error is 6203
```

Solutions to Exercise 5 (cont.)

- Obtain the mean squared error of these predictions and also an error scatter plot.

```
library(ggplot2)
ggplot(data.frame(Predictions=preds,Trues=ts$medv),aes(x=Predictions,y=Trues)) +
  geom_point() + geom_smooth(method='loess') +
  geom_abline(slope=1, intercept=0,color="red") + ggtitle("The Errors Scatter Plot")
```



Hands on Tree-based Models - the Wines data

File `Wine.Rdata` contains two data frames with data on green wine quality: (i) `redWine` and (ii) `whiteWine`. Each of these data sets contains a series of tests with green wines (red and white). For each of these tests the values of several physicochemical variables together with a quality score assigned by wine experts (column `quality`).

- 1 Build a regression tree for the white wines data set [solution](#)
- 2 Obtain a graph of the obtained regression tree [solution](#)
- 3 Apply the tree to the data used to obtain the model and calculate the mean squared error of the predictions [solution](#)
- 4 Split the data set in two parts: 70% of the tests and the remaining 30%. Using the larger part to obtain a regression tree and apply it to the other part. Calculate again the mean squared error. Compare with the previous scores and comment. [solution](#)

Solutions Exercise 1

- Build a regression tree for the white wines data set

```
load("Wine.Rdata")
library(DMwR2)
```

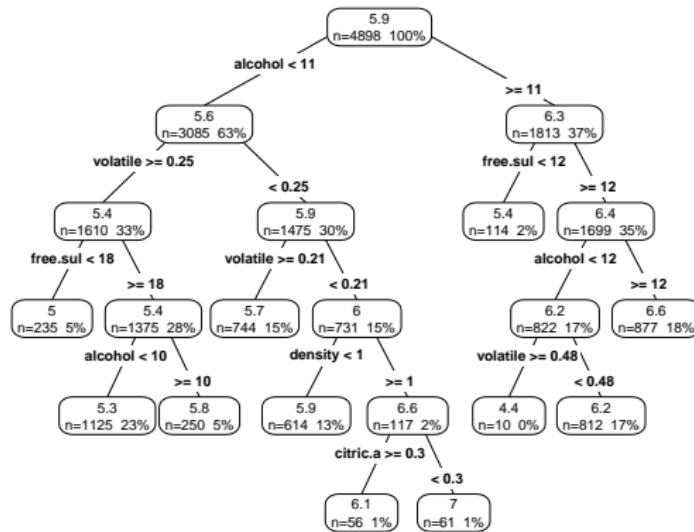
```
ab <- rpartXse(quality ~ ., whiteWine)
```

Go back

Solutions Exercise 2

- Obtain a graph of the obtained regression tree

```
library(rpart.plot)
prp(ab, type=4, extra=101)
```



Solutions Exercise 3

- Apply the tree to the data used to obtain the model and calculate the mean squared error of the predictions

```
prevs <- predict(ab,whiteWine)
mse <- mean((whiteWine$quality - prevs)^2)
mse

## [1] 0.5382
```

[Go back](#)

Solutions Exercise 4

- Split the data set in two parts: 70% of the tests and the remaining 30%. Using the larger part to obtain a regression tree and apply it to the other part. Calculate again the mean squared error. Compare with the previous scores and comment.

```
xs <- sample(1:nrow(whiteWine), as.integer(0.7*nrow(whiteWine)))
train <- whiteWine[xs,]
test <- whiteWine[-xs,]
ab2 <- rpartXse(quality ~.,train)
prevs2 <- predict(ab2,test)
mse2 <- mean((test$quality - prevs2)^2)
c(before=mse,now=mse2)

##      before      now
## 0.5382229 0.6037395
```

[Go back](#)

Hands on SVMs

The file `Wine.Rdata` contains 2 data frames with data about the quality of “green” wines: i) `redWine` and ii) `whiteWine`. Each of these data sets has information on a series of wine tasting sessions to “green” wines (both red and white). For each wine sample several physico-chemical properties of the wine sample together with a quality score assigned by a committee of wine experts (variable `quality`).

- 1 Obtain and SVM for forecasting the quality of the red variant of “green” wines [solution](#)
- 2 Split the data set in two parts: one with 70% of the samples and the other with the remaining 30%. Obtain an SVM with the first part and apply it to the second. What was the resulting mean absolute error? [solution](#)
- 3 Using the `round()` function, round the predictions obtained in the previous question to the nearest integer. Calculate the error rate of the resulting integers when compared to the true values [solution](#)

Solutions to Exercise 1

- Obtain and SVM for forecasting the quality of the red variant of “green” wines

```
load("Wine.Rdata")
library(e1071)
```

```
s <- svm(quality ~ ., redWine)
```

[Go back](#)

Solutions to Exercise 2

- Split the data set in two parts: one with 70% of the samples and the other with the remaining 30%. Obtain an SVM with the first part and apply it to the second. What was the resulting mean absolute error?

```
xs <- sample(1:nrow(redWine),  
             as.integer(0.7*nrow(redWine)))  
train <- redWine[xs,]  
test <- redWine[-xs,]  
s2 <- svm(quality ~.,train)  
p2 <- predict(s2,test)  
mae <- mean(abs(test$quality - p2))  
mae  
  
## [1] 0.4358064
```

[Go back](#)

Solutions to Exercise 3

- Using the `round()` function, round the predictions obtained in the previous question to the nearest integer. Calculate the error rate of the resulting integers when compared to the true values

```
pi2 <- round(p2)
mc <- table(pi2,test$quality)
mc

##  
##   pi2    3     4     5     6     7     8  
##   5     2     9  165    60     1     0  
##   6     0     4    41   114    36     4  
##   7     0     0     2    18    23     1
```

Solutions to Exercise 3 (cont.)

```
pi3 <- factor(pi2, levels=levels(factor(test$quality)))
mc2 <- table(pi3,test$quality)
mc2

##
## pi3    3     4     5     6     7     8
##   3    0     0     0     0     0     0
##   4    0     0     0     0     0     0
##   5    2     9   165    60     1     0
##   6    0     4    41   114    36     4
##   7    0     0     2    18    23     1
##   8    0     0     0     0     0     0

err <- 1-sum(diag(mc2))/sum(mc2)
err

## [1] 0.3708333
```

Is this as bad as it looks like?

Go back



Hands on Linear Regression and Random Forests

the Algae data set

Load in the data set `algae` from package **DMwR2** and answer the following questions:

- 1 How would you obtain a random forest to forecast the value of alga `a4` [solution](#)
- 2 Repeat the previous exercise but now using a linear regression model. Try to simplify the model using the `step()` function. [solution](#)
- 3 Obtain the predictions of the two previous models for the data used to obtain them. Draw a scatterplot comparing these predictions [solution](#)
- 4 The data frame named `test.algae` contains a test set with some extra 140 water samples for which we want predictions. Use the previous two models to obtain predictions for `a4` on these new samples. Check what happened to the test cases with NA's. Fill-in the NA's on the test set and repeat the experiment. [solution](#)



Solutions to Exercise 1

- How would you obtain a random forest to forecast the value of alga a4

```
library(randomForest)
library(DMwR2)
data(algae)
algae <- algae[-c(62,199),]
algae <- knnImputation(algae)
rf.a4 <- randomForest(a4 ~.,algae[,c(1:11,15)])
```

[Go back](#)

Solutions to Exercise 2

- Repeat the previous exercise but now using a linear regression model. Try to simplify the model using the `step()` function.

```
lm.a4 <- lm(a4 ~ ., algae[, c(1:11, 15)])
```

```
lm.a4 <- step(lm.a4)
```

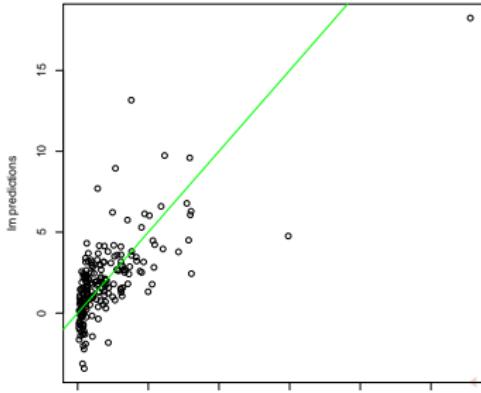
```
lm.a4
```

```
## 
## Call:
## lm(formula = a4 ~ mxPH + mnO2 + NO3 + NH4 + PO4, data = algae[,
##       c(1:11, 15)])
## 
## Coefficients:
## (Intercept)          mxPH          mnO2          NO3          NH4
## 25.155775     -2.564539     -0.307999     -0.466876     0.000932
##          PO4
##         0.009314
```

Solutions to Exercise 3

- Obtain the predictions of the two previous models for the data used to obtain them. Draw a scatterplot comparing these predictions

```
psrf <- predict(rf.a4, algae)
pslm <- predict(lm.a4, algae)
plot(psrf, pslm, xlab="Random forest predictions", ylab="lm predictions")
abline(0,1,col="green")
```



Solutions to Exercise 4

- The data frame named `test.algae` contains a test set with some extra 140 water samples for which we want predictions. Use the previous two models to obtain predictions for `a4` on these new samples.

```
prevs.rf <- predict(rf.a4,test.algae)
prevs.lm <- predict(lm.a4,test.algae)
summary(prevs.rf)

##      Min. 1st Qu. Median      Mean 3rd Qu.      Max.    NA's
## 0.09421  0.83539  1.56449  2.12729  2.45076 21.66409      18

summary(prevs.lm) # notice the difference in the number of NA's. Why?
```

```
##      Min. 1st Qu. Median      Mean 3rd Qu.      Max.    NA's
## -2.8201  0.5774  1.5603  2.2330  3.3549 28.6980      6
```

Solutions to Exercise 4 (cont.)

```
test.algae <- knnImputation(test.algae, distData=algae[, 1:11])
prevs.rf <- predict(rf.a4, test.algae)
prevs.lm <- predict(lm.a4, test.algae)
```

Hands on Mars and Gradient Boosting

Load in the data set `Boston_Housing` from package **MASS** and answer the following questions:

- 1 Split the data set into training and testing sets and obtain a MARS model and a GBM model with the training set. [solution](#)
- 2 Check the predictions of the models on the test set. Obtain their mean squared error. [solution](#)
- 3 Read the help pages of the two functions that obtain MARS and GBM and explore a few variants of these models and check the results in terms of the performance on the test set [solution](#)
- 4 Produce a barplot with the errors of the different variants you have considered. [solution](#)

Solutions to Exercise 1

- Split the data set into training and testing sets and obtain a MARS model and a GBM model with the training set.

```
library(gbm)
library(earth)
data(Boston, package="MASS")
set.seed(1234)
trPerc <- 0.7
sp <- sample(1:nrow(Boston), as.integer(trPerc*nrow(Boston)))
tr <- Boston[sp,]
ts <- Boston[-sp,]
b <- gbm(medv ~ ., distribution='gaussian', data=tr, n.trees=5000, verbose=F)
m <- earth(medv ~ ., tr, degree=2)
```

[Go back](#)

Solutions to Exercise 2

- Check the predictions of the models on the test set. Obtain their mean squared error.

```
pb <- predict(b, ts, n.trees=5000)
mean( (pb-ts$medv)^2)

## [1] 20.96

pm <- predict(m, ts)
mean( (pm-ts$medv)^2)

## [1] 19.9
```

[Go back](#)

Solutions to Exercise 3

- Explore a few variants of these models and check the results in terms of the performance on the test set

```
varsb <- expand.grid(n.trees=c(5000, 7500, 15000), interaction.depth=c(1, 2),
                      shrinkage=c(0.001, 0.05))
varsm <- expand.grid(degree=c(1, 2, 3), thresh=c(0.001, 0.05, 0.01),
                      fast.k=c(20, 30))
nvars <- nrow(varsb)
nreps <- 10
trPerc <- 0.7
res <- matrix(NA, nrow=nvars*2, ncol=2)
```

Solutions to Exercise 3 (cont.)

```

set.seed(1234)
for(v in 1:nvars) {
  errs <- matrix(NA, nrow=nreps, ncol=2)
  for(r in 1:nreps) {
    sp <- sample(1:nrow(Boston), as.integer(trPerc*nrow(Boston)))
    tr <- Boston[sp,]
    ts <- Boston[-sp,]
    b <- gbm(medv ~ ., distribution='gaussian', data=tr,
              n.trees=varsb[v, "n.trees"],
              interaction.depth=varsb[v, "interaction.depth"],
              shrinkage=varsb[v, "shrinkage"], verbose=FALSE)
    pb <- predict(b, ts, n.trees=varsb[v, "n.trees"])
    m <- earth(medv ~ ., tr,
                degree=varsm[v, "degree"],
                thresh=varsm[v, "thresh"],
                fast.k=varsm[v, "fast.k"]
               )
    pm <- predict(m, ts)
    errs[r, 1] <- mean((pb-ts$medv)^2)
    errs[r, 2] <- mean((pm-ts$medv)^2)
  }
  res[v, ] <- c(mean(errs[, 1]), sd(errs[, 1]))
  res[nvars+v, ] <- c(mean(errs[, 2]), sd(errs[, 2]))
}

```

[Go back](#)

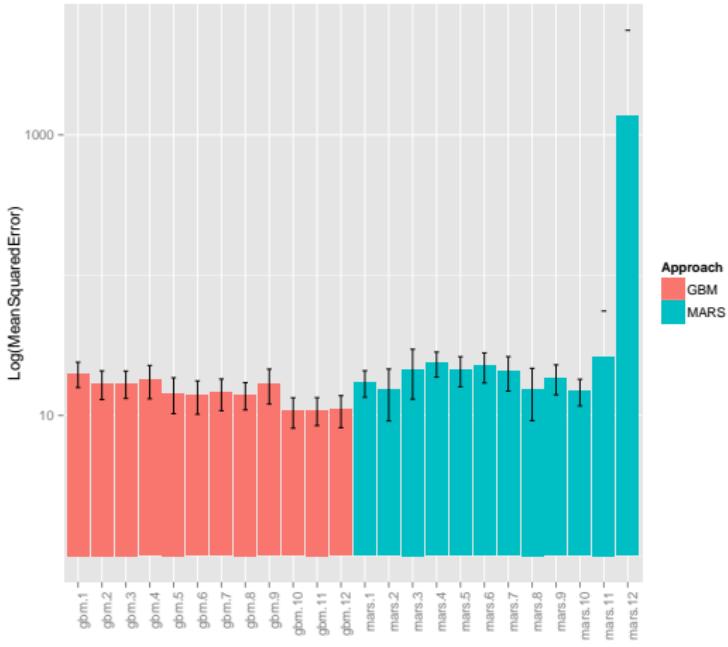
Solutions to Exercise 4

- Produce a barplot with the errors of the different variants you have considered.

```
library(ggplot2)
colnames(res) <- c("AvgErr", "SdErr")
results <- data.frame(System=c(paste("gbm", 1:nvars, sep="."),
                                paste("mars", 1:nvars, sep=".")), res)
results$Approach <- c(rep("GBM", nvars), rep("MARS", nvars))
results$System <- factor(results$System, levels=results$System)
ggplot(data=results, aes(x=System, y=AvgErr, fill=Approach)) +
  geom_bar(stat="identity") +
  geom_errorbar(aes(ymax = AvgErr + SdErr, ymin=AvgErr - SdErr), width=0.2) +
  theme(axis.text.x = element_text(angle = 90, hjust = 1),
        axis.title.x = element_blank())
```

Solutions to Exercise 4 (cont.)

```
## Warning:  NaNs produced
## Warning:  Removed 4 rows containing missing values (geom_path).
## Warning:  Removed 4 rows containing missing values (geom_path).
```



Hands on Performance Estimation

the Algae data set

Load in the data set `algae` and answer the following questions:

- 1 Estimate the MSE of a regression tree for forecasting alga `a1` using 10-fold Cross validation. [solution](#)
- 2 Repeat the previous exercise this time trying some variants of random forests. Check what are the characteristics of the best performing variant. [solution](#)
- 3 Compare the results in terms of mean absolute error of the default variants of a regression tree, a linear regression model and a random forest, in the task of predicting alga `a3`. Use 2 repetitions of a 5-fold Cross Validation experiment. [solution](#)
- 4 Carry out an experiment designed to select what are the best models for each of the seven harmful algae. Use 10-fold Cross Validation. For illustrative purposes consider only the default variants of regression trees, linear regression and random forests. [solution](#)

Solutions to Exercise 1

- Estimate the MSE of a regression tree for forecasting alga *a1* using 10-fold Cross validation.

```
library(DMwR)
library(performanceEstimation)
data(algae)
algae <- algae[-c(62, 199), ]
res.a1 <- performanceEstimation(
  PredTask(a1 ~ ., algae[, 1:12], "algaA1"),
  Workflow("standardWF", learner="rpartXse", pre="knnImp"),
  EstimationTask("mse", method=CV()))
)
```

Solutions to Exercise 1 (cont.)

- Estimate the MSE of a regression tree for forecasting alga *a1* using 10-fold Cross validation.

```
summary(res.a1)

##
## == Summary of a Cross Validation Performance Estimation Experiment ==
##
## Task for estimating mse using
## 1 x 10 - Fold Cross Validation
## Run with seed = 1234
##
## * Predictive Tasks :: algaA1
## * Workflows  :: standardWF
##
## -> Task: algaA1
##   *Workflow: standardWF
##           mse
## avg     321.10
## std     200.70
## med     302.53
## iqr     302.49
## min     96.22
## max    637.87
## invalid 0.00
```

Solutions to Exercise 2

- Repeat the previous exercise this time trying some variants of random forests. Check what are the characteristics of the best performing variant.

```
library(randomForest)
resrf.al <- performanceEstimation(
  PredTask(al ~ ., algae[, 1:12], "algaA1"),
  workflowVariants("standardWF",
    learner="randomForest",
    learner.pars=list(ntree=c(500, 750, 1000)),
    pre="knnImp"),
  EstimationTask("mse", method=CV())
)
```

Solutions to Exercise 2 (cont.)

```
summary(resrf.a1)

##
## == Summary of a Cross Validation Performance Estimation Experiment ==
##
## Task for estimating mse using
## 1 x 10 - Fold Cross Validation
## Run with seed = 1234
##
## * Predictive Tasks :: algaA1
## * Workflows :: randomForest.v1, randomForest.v2, randomForest.v3
##
## -> Task: algaA1
##   *Workflow: randomForest.v1
##     mse
##   avg      255.79
##   std      167.89
##   med      200.92
##   iqr      178.99
##   min      73.26
##   max      640.69
##   invalid   0.00
##
##   *Workflow: randomForest.v2
##     mse
##   avg      256.09
##   std      166.75
##   med      203.92
##   iqr      172.09
##   min      74.05
```



Solutions to Exercise 2 (cont.)

- Repeat the previous exercise this time trying some variants of random forests. Check what are the characteristics of the best performing variant.

```
topPerformer(resrf.al, "mse", "algaA1")  
  
## Workflow Object:  
##   Workflow ID      :: randomForest.v1  
##   Workflow Function :: standardWF  
##   Parameter values:  
##     learner.pars  -> ntree=500  
##     learner      -> randomForest
```

[Go back](#)

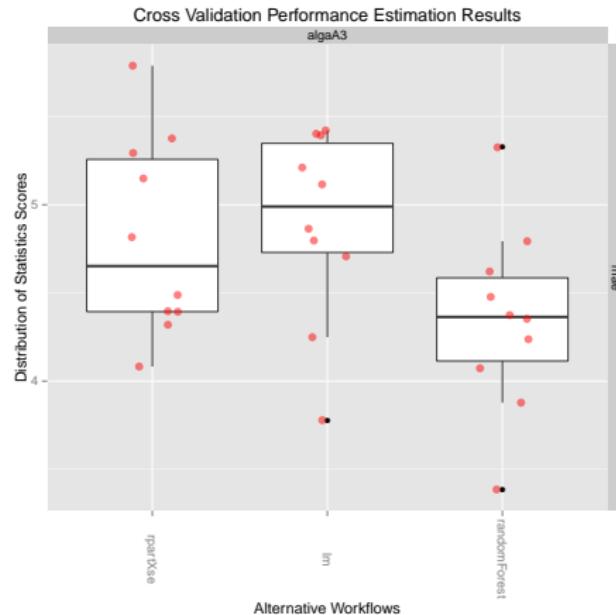
Solutions to Exercise 3

- Compare the results in terms of mean absolute error of the default variants of a regression tree, a linear regression model and a random forest, in the task of predicting alga a3. Use 2 repetitions of a 5-fold Cross Validation experiment. Plot the results

```
res.a3 <- performanceEstimation(  
  PredTask(a3 ~ ., algae[,c(1:11,14)], "algaA3") ,  
  workflowVariants("standardWF",  
    learner=c("rpartXse", "lm", "randomForest") ,  
    pre="knnImp") ,  
  EstimationTask("mae", method=CV(nReps=2, nFolds=5))  
)
```

Solutions to Exercise 3 (cont.)

```
plot(res.a3)
```



Go back

Solutions to Exercise 4

- Carry out an experiment designed to select what are the best models for each of the seven harmful algae. Use 10-fold Cross Validation. For illustrative purposes consider only the default variants of regression trees, linear regression and random forests.

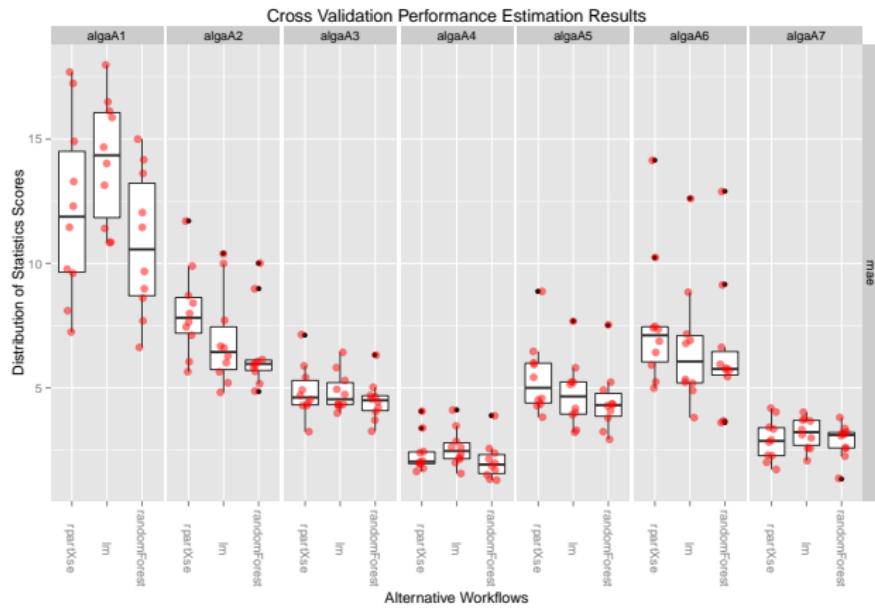
```

tgts <- 12:18
tasks <- c()
for(t in tgts)
  tasks <- c(tasks,
             PredTask(as.formula(paste(colnames(algae)[t], '~ .')),
                       algae[,c(1:11,t)],
                       paste0("algaeA",t-11),
                       copy=TRUE))
res.algae <- performanceEstimation(
  tasks,
  workflowVariants(learner=c("rpartXse", "lm", "randomForest"),
                   pre="knnImp"),
  EstimationTask("mae", method=CV())
)

```

Solutions to Exercise 4 (cont.)

```
plot(res.algae)
```



Solutions to Exercise 4 (cont.)

```
topPerformers(res.algae)

## $algaA1
##           Workflow Estimate
## mae randomForest    10.785
##
## $algaA2
##           Workflow Estimate
## mae randomForest     6.461
##
## $algaA3
##           Workflow Estimate
## mae randomForest     4.486
##
## $algaA4
##           Workflow Estimate
## mae randomForest     2.059
##
## $algaA5
##           Workflow Estimate
## mae randomForest     4.466
##
## $algaA6
##           Workflow Estimate
## mae randomForest     6.453
##
## $algaA7
##           Workflow Estimate
## mae randomForest     2.855
```

Hands on Statistical Significance

Using the *algae* data set from package **DMwR2** answer the following questions

- 1 For the 7 different algae, choose a reasonable set of SVM variants and estimate their MSE error. [solution](#)
- 2 Check if these alternatives are significantly better than the SVM with the default parameter settings [solution](#)
- 3 Present the results of the previous question visually [solution](#)

Solutions to Exercise 1

- Check which workflow achieved the best score and carry out a paired comparison of the other alternatives against this workflow

```

library(performanceEstimation)
library(e1071)
data(algae, package="DMwR2")
tgts <- 12:18
tasks <- c()
for(t in tgts)
  tasks <- c(tasks,
             PredTask(as.formula(paste(colnames(algae)[t], '~ .'))),
             algae[,c(1:11,t)],
             paste0("algaA", t-11),
             copy=TRUE))
res.algae <- performanceEstimation(
  tasks,
  c(Workflow(learner="svm", pre="knnImp", wfID="defaultSVM"),
    workflowVariants(learner="svm",
                      learner.pars=list(cost=c(1,3,5,10,15), gamma=c(0.01,0.05),
                                         epsilon=c(0.01,0.05)),
                      pre="knnImp")),
    ),
  EstimationTask("mse", method=CV())
)

```

[Go Back](#)

Solutions to Exercise 2

```
pcomp <- pairedComparisons(res.algae, baseline="defaultSVM")
pcomp$mse$F.test

## $chi
## [1] 42.07792
##
## $FF
## [1] 2.578249
##
## $critVal
## [1] 1.205512
##
## $rejNull
## [1] TRUE
```

Solutions to Exercise 2

```
pcomp$mse$BonferroniDunn.test

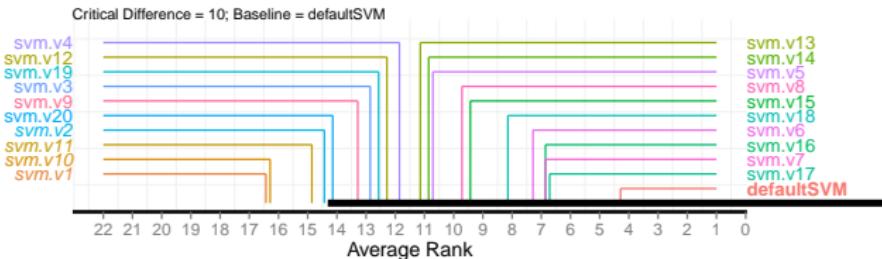
## $critDif
## [1] 10.02729
##
## $baseline
## [1] "defaultSVM"
##
## $rkDifs
##    svm.v1    svm.v2    svm.v3    svm.v4    svm.v5    svm.v6    svm.v7
## 12.142857 10.142857  8.571429  7.571429  6.428571  3.000000  2.571429
##    svm.v8    svm.v9    svm.v10   svm.v11   svm.v12   svm.v13   svm.v14
##  5.428571  9.000000 12.000000 10.571429  8.000000  6.857143  6.571429
##    svm.v15   svm.v16   svm.v17   svm.v18   svm.v19   svm.v20
##  5.142857  2.571429  2.428571  3.857143  8.285714  9.857143
##
## $signifDifs
##    svm.v1    svm.v2    svm.v3    svm.v4    svm.v5    svm.v6    svm.v7    svm.v8    svm.v9
##    TRUE     TRUE    FALSE    FALSE    FALSE    FALSE    FALSE    FALSE    FALSE
##    svm.v10   svm.v11   svm.v12   svm.v13   svm.v14   svm.v15   svm.v16   svm.v17   svm.v18
##    TRUE     TRUE    FALSE    FALSE    FALSE    FALSE    FALSE    FALSE    FALSE
##    svm.v19   svm.v20
##    FALSE    FALSE
```

[Go Back](#)

Solutions to Exercise 3

- Decide on a p-value and check which differences are statistically significant

```
CDdiagram.BD( pcomp )
```

[Go Back](#)