

Fundamentals of Computational Neuroscience 2e

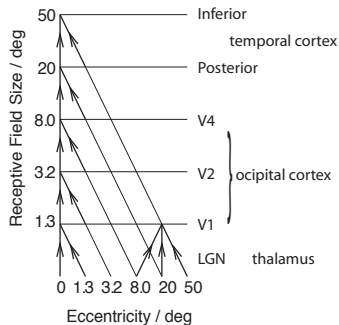
Thomas Trappenberg

March 28, 2009

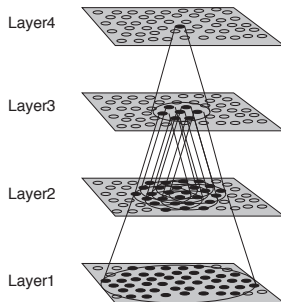
Chapter 10: The cognitive brain

Hierarchical maps and attentive vision

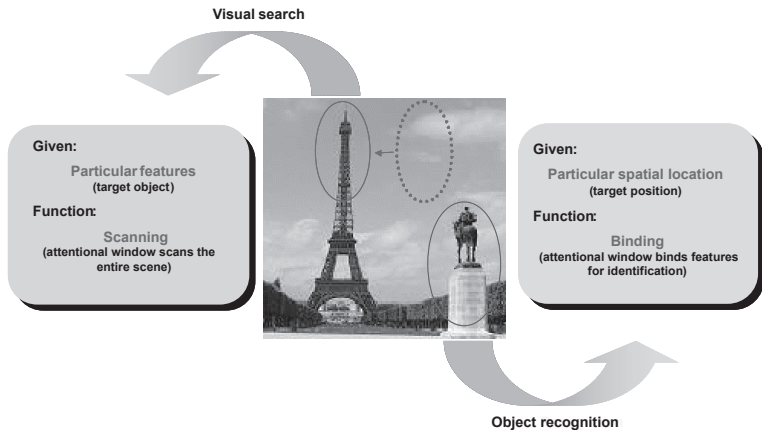
A. Ventral visual pathway



B. Layered cortical maps

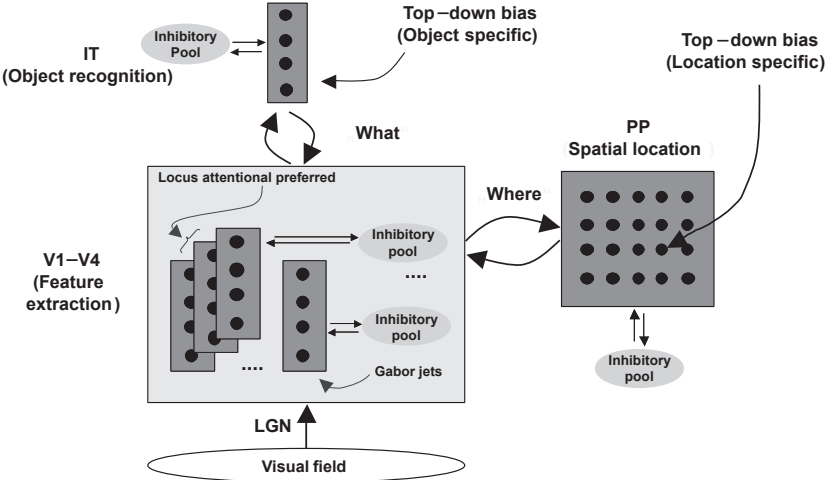


Attention in visual search and object recognition



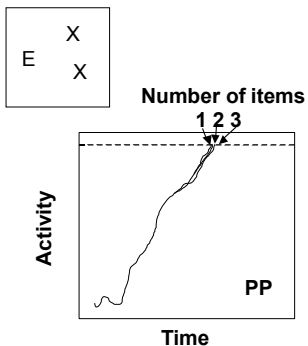
Gustavo Deco

Model

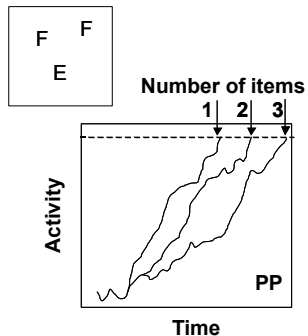


Example results

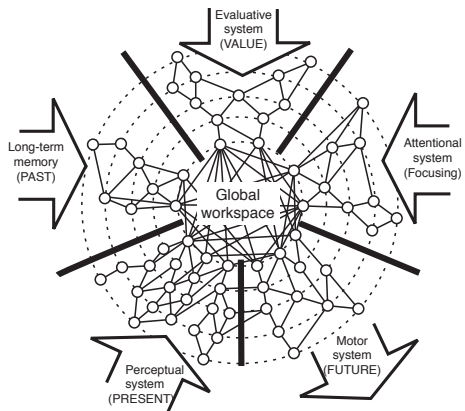
A. "Parallel search"



B. "Serial search"



The interconnecting workspace hypothesis

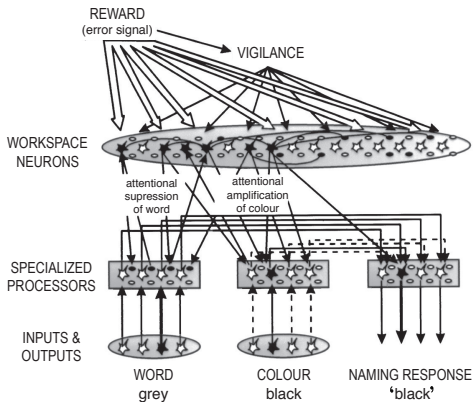


Stroop task modelling

A. Stroop task

task \ image	word naming	colour naming
grey	grey	black
black	black	grey

B. Workspace model for stroop task

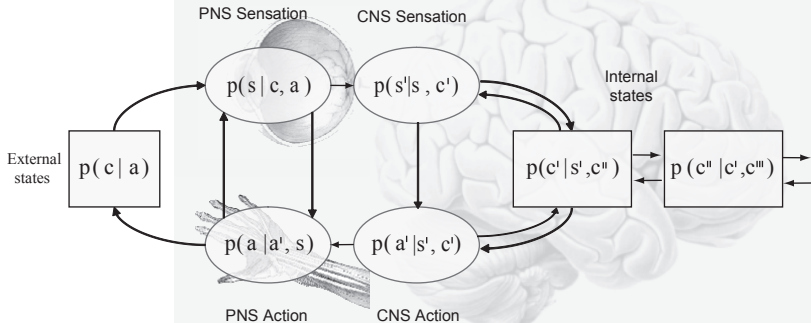


The anticipating brain

1. The brain can develop a model of the world, which can be used to anticipate or predict the environment.
2. The inverse of the model can be used to recognize causes by evoking internal concepts.
3. Hierarchical representations are essential to capture the richness of the world.
4. Internal concepts are learned through matching the brain's hypotheses with input from the world.
5. An agent can learn actively by testing hypothesis through actions.
6. The temporal domain is an important degree of freedom.

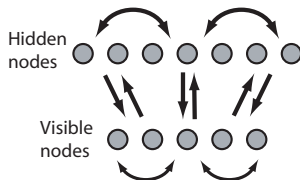
Environment

Agent



Recurrent networks with hidden nodes

The Boltzmann machine:



$$\text{Energy: } H^{nm} = -\frac{1}{2} \sum_{ij} w_{ij} s_i^n s_j^m$$

$$\text{Probabilistic update: } p(s_i^n = +1) = \frac{1}{1 + \exp(-\beta \sum_j w_{ij} s_j^n)}$$

$$\text{Boltzmann-Gibbs distribution: } p(\mathbf{s}^v; \mathbf{w}) = \frac{1}{Z} \sum_{m \in h} \exp(-\beta H^{vm})$$

Training Boltzmann machine

Kulbach-Leibler divergence

$$\begin{aligned}\text{KL}(p(\mathbf{s}^V), p(\mathbf{s}^V; \mathbf{w})) &= \sum_{\mathbf{s}} p(\mathbf{s}^V) \log \frac{p(\mathbf{s}^V)}{p(\mathbf{s}^V; \mathbf{w})} \\ &= \sum_{\mathbf{s}} p(\mathbf{s}^V) \log p(\mathbf{s}^V) - \sum_{\mathbf{s}} p(\mathbf{s}^V) \log p(\mathbf{s}^V; \mathbf{w})\end{aligned}$$

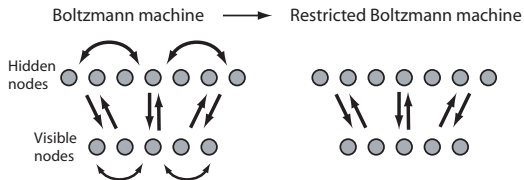
Minimizing KL is equivalent to maximizing the average log-likelihood function

$$l(\mathbf{w}) = \sum_{\mathbf{s}} p(\mathbf{s}^V) \log p(\mathbf{s}^V; \mathbf{w}) = \langle \log p(\mathbf{s}^V; \mathbf{w}) \rangle.$$

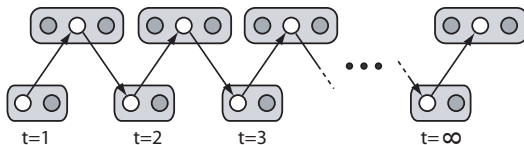
Gradient decent \rightarrow Boltzmann Learning

$$\Delta w_{ij} = \eta \frac{\partial l}{\partial w_{ij}} = \eta \frac{\beta}{2} (\langle s_i s_j \rangle_{\text{clamped}} - \langle s_i s_j \rangle_{\text{free}}).$$

The restricted Boltzmann machine



Contrastive Hebbian learning: Alternating Gibbs sampling



Concept input

Recognition readout and stimulation

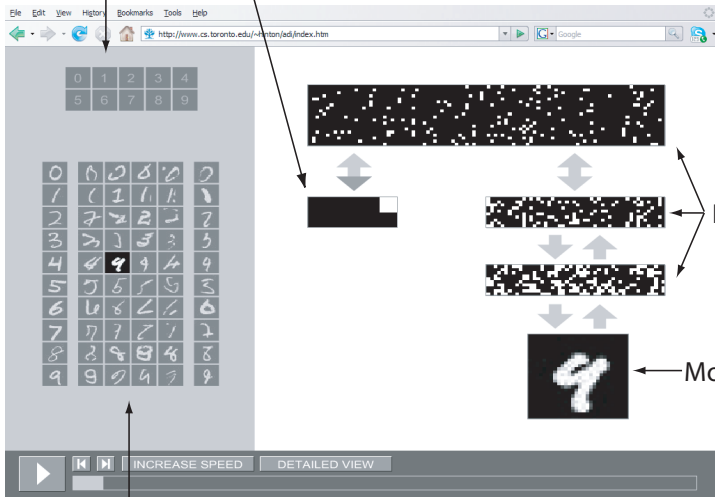


Image input