Improved Data Partitioning For Building Large ROLAP Data Cubes in Parallel

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Abstract

The pre-computation of data cubes is critical to improving the response time of On-Line Analytical Processing (OLAP) systems and can be instrumental in accelerating data mining tasks in large data warehouses. However, as the size of data warehouses grows, the time it takes to perform this pre-computation becomes a significant performance bottleneck.

This paper presents an *improved* parallel method for generating ROLAP data cubes on a shared-nothing multiprocessor based on a novel *optimized* data partitioning technique. Since no shared disk is required, our method can be used for highly scalable processor clusters consisting of standard PCs with local disks only, connected via a data switch. The approach taken, which uses a ROLAP representation of the data cube, is well suited for large data warehouses and high dimensional data, and supports the generation of both fully materialized and partially materialized data cubes.

We have implemented our new parallel shared-nothing data cube generation method and evaluated the impact of our novel *optimized* data partitioning technique. The experiements show a significant performace improvement. As a result, our new optimized parallel data cube generation method achieves close to optimal speedup for as many as 32 processors, generating a full data cube for a fact table with 16 million rows and 8 attributes in under 7 minutes. For a fact table with 256 million rows and 8 attributes, our improved method reaches optimal speedup for 32 processors, generating a full data cube consisting of \approx 7 billion rows (200 Gigabytes) in under 88 minutes. In comparison with previous approaches, our new method does significantly improve the scalability with respect to both, the number of processors and the I/O bandwidth (number of parallel disks).

Keywords: Data Cube, ROLAP, Parallel Computing.

INTRODUCTION

The pre-computation of the different views (group-bys) of a data cube, i.e. the forming of aggregates for every combination of GROUP-BY attributes, is critical to improving the response time of On-Line Analytical Processing (OLAP) queries in decision support systems and can be instrumental in accelerating data mining tasks in large data warehouses (Han, et.al., 1996). As the size of data warehouses grows, the time it takes to perform this pre-computation becomes a significant performance bottleneck, one which may stretch into days in the very largest cases (Microsoft, 2001). This paper presents an *improved* parallel method for generating ROLAP data cubes on shared-nothing multiprocessors, based on a novel *optimized* data partitioning technique. Since no shared disk is required, this method can be applied to highly scalable processor clusters consisting of standard PCs with local disks, connected via a high bandwidth (Ethernet) switch. Parallelism based on such shared-nothing machines is an attractive solution to improving system performance especially in the context of large data warehouses where scaling I/O bandwidth to disk is as important as scaling computational resources.

For a given raw data set, R, with N records and d attributes (dimensions), a view is constructed by an aggregation of R along a subset of attributes. As proposed in (Gray, et.al., 1997), the pre-computation of the full data cube (the set of all 2^d possible views) or a partial data cube (a subset of all 2^d possible views) supports the fast execution of subsequent OLAP queries. Many methods have been presented for generating the data cube on sequential (Beyer & Ramakrishnan, 1999; Harinarayan, et.al., 1996; Ross & Srivastava, 1997; Sarawagi, et.al., 1996; Yu & Lu, 2001; Zhao, et.al., 1997) and parallel systems (Chen, et.al. 2004; Dehne, et.al. 2001; Dehne, et.al. 2002; Goil & Choudhary, 1997; Goil & Choudhary, 1999; Lu, et.al., 1997; Muto & Kitsuregawa, 1999; Ng, et.al., 2001). For parallel data cube construction, good data partitioning is a key factor in obtaining good performance on shared nothing multiprocessors. Some researchers partition data on one or several dimensions (Goil & Choudhary, 1998; Muto & Kitsuregawa, 1999). They assume that the product of the cardinalities of these dimensions is much larger than the number of processors (Goil & Choudhary, 1998) in order to achieve sufficient parallelism. The advantage of their method is that they do not need to merge views across the network. However, in practice, this assumption is often not true. The cardinality of some dimensions may be small, such as gender, months and intervals for a numeric attribute. Therefore, those methods are often not scalable. One approach which avoids these problems is to partition on all dimensions and then apply a parallel merge procedure (Chen, et.al. 2004). The challenge here is that merge procedures based on fixed data partitioning schemes often lead to excess inter-processor communications which may greatly reduce the speedup achieved by the parallel system and limit its effective scalability.

In this paper, we describe and evaluate a novel optimized data partition scheme for parallel ROLAP data cube generation which improves significantly on our previous result in (Chen, et.al. 2004) and outperforms all previously reported parallel data cube generation methods. Our new dynamic data partitioning scheme adapts to both, the current data set and the performance parameters of the parallel machine. Using this scheme, data cube generation tasks involving millions of rows of input, which take days to perform on a single processor machine, can be completed in just hours on a 32 processor cluster. We have performed an extensive performance evaluation of our new method, exploring relative speedup, scaleup, sizeup, output sizes and data skew. For our experiments, our new optimized data partitioning method results in approximately twice the speedup achieved with our previous fixed data partitioning scheme (Chen, et.al. 2004) which had already outperformed all previously reported parallel data cube generation methods (Dehne, et.al. 2002; Chen, et.al. 2004). Our new optimized data partition scheme exhibited optimal, linear, speedup for full cube generation on as many as 32 processors, as well as excellent sizeup and scaleup behavior. For example, for a fact table with 16 million rows and 8 attributes, our parallel data cube generation method achieves close to optimal speedup for 32 processors, generating a full data cube in under 7 minutes. For a fact table with 256 million rows and 8 attributes, our parallel method achieves optimal speedup for 32 processors, generating a full data cube consisting of ≈ 7 billion rows (200 Gigabytes) in under 88 minutes.

In comparison with previous approaches, our new method has a significantly better scalability with respect to the number of processors. Optimal speedup for as many as 32 processors was not observed for any previous parallel method (Chen, et.al. 2004; Dehne, et.al. 2001; Dehne, et.al. 2002; Goil & Choudhary, 1997; Goil & Choudhary, 1999; Lu, et.al., 1997; Muto & Kitsuregawa, 1999; Ng, et.al., 2001). In addition, because of its shared nothing approach, our new method does also significantly improve the scalability with respect to the I/O bandwidth (number of parallel disks) which is of great importance for handling large data sets.

The remainder of this paper is organized as follows. In the following section we review the global structure of our algorithm which is similar to (Chen, et.al. 2004). We then present

in detail our new *optimized* data partitioning method, the main contribution of this paper. The performance improvement achieved by our new optimized method is discussed in the subsequent sections.

PARALLEL DATA CUBE CONSTRUCTION FOR SHARED-NOTHING MULTIPROCESSORS

We first review the global structure of our parallel data cube construction algorithm for shared-nothing multiprocessors, which is similar to (Chen, et.al. 2004). Consider a raw data set R with N rows and d attributes D_l , ..., D_d . Without loss of generality, let $|D_1| \ge |D_2| \ge ... \ge |D_d|$, where $|D_i|$ is the cardinality for dimension D_i , $1 \le i \le d$ (i.e. the number of distinct values for dimension D_i). Let S be the set of all S view identifiers. Each view identifier consists of a subset of S and S are refer to the latter case as S and S are refer to the latter case as S and S are refer to the latter case as S are refer to the S as shown in Figure 1b. The goal is to create a data cube S containing the views in S. We assume that, when the algorithm terminates, every view is distributed evenly across the S as shown in Figure 1b. It is important to note that, for the subsequent use of the views by OLAP queries, each view needs to be evenly distributed across all disks in order to achieve maximum I/O bandwidth for subsequent parallel disk accesses.

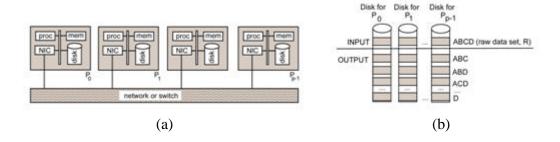


Figure 1: (a) Shared-Nothing Multiprocessor. (b) Data Partitioning.

The basic communication operation used by our parallel data cube algorithm is the hrelation (method MPI_ALL_TO_ALL_v in MPI). In addition, our method uses two basic

sequential local disk operations, applied by each processor to its local disk: (1) linear scan and (2) external memory sort (Vitter, 2001). For a processor P_j with local memory size M and a local disk with block transfer size B, a linear scan through a file of size N stored on its disk requires O(N/B) block transfers between disk and memory while an external memory sort of that file requires $O(N/B \log_{M/B}(N/B))$ block transfers (Vitter, 2001). We will present our method for a shared-nothing multiprocessor with one local disk per processor P_j . However, it is easy to generalize our methods for machines with multiple local disks per processor by applying the linear scan and external memory sort methods for a single processor with multiple local disks presented in (Vitter & Shriver, 1994).

Let $S_i \subset S$ be the subset of view identifiers in S that start with D_i , and let DC_i be the data cube for S_i . DC_i is called the *i-subcube* and the view $D_i...D_d$ is referred to as $Root_i$; see Figure 2. As discussed above, all data sets are distributed over the p disks of the p processors as shown in Figure 1b. We refer to the part of a data set stored on processor P_j as its j-partition. The j-partitions of R, DC_i , and $Root_i$ are denoted as R_j , DC_{ij} , and $Root_{ij}$, respectively.

Algorithm 1 describes the global structure of our parallel data cube construction algorithm for shared-nothing multiprocessors. The algorithm consists of d iterations i=1...d. In iteration i, the i-subcube DC_i is created in five main steps: Computing $Root_i$, computing the schedule tree T_i , optimizing the partitioning of $Root_i$ into $Root_{i1}$... $Root_{ip}$, computing the local DC_{ij} from each $Root_{ij}$, and merging the DC_{ij} to obtain the correct i-subcube DC_i .

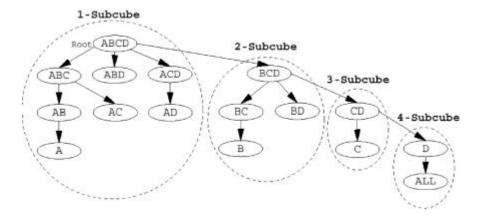


Figure 2: Subcubes of a data cube for d=4. Dimensions are labelled D_1 ="A", D_2 ="B", D_3 ="C", D_4 ="D".

Algorithm 1: Parallel-Shared-Nothing-Data-Cube

INPUT: R, the raw data set; N, the number of rows in R; d, the number of attributes; p, the number of processors; S, the set of views to be generated. Every processor P_j $(1 \le j \le p)$ stores on its disk a set R_j of N/p rows of R.

OUTPUT: DC, the data cube distributed over the p processors. Each view is evenly distributed over the p processors' disks.

- 1: **FOR** i=1 to d
- 2: Compute $Root_i$ via a parallel global sort of $Root_{i-1}$ by key D_i , ..., D_d , where $Root_0=R$. As a result, each processor P_i stores a j-partition, $Root_{ij}$, of $Root_i$.
- 3: Processor P_0 generates and broadcasts the schedule tree, T_i , for computing S_i from $Root_i$.
- 4: Execute Optimize- $Partition(Root_i)$ to obtain an optimized partitioning of $Root_i$ into $Root_{ij}$, $1 \le j \le p$.
- 5: Every processor P_j $(1 \le j \le p)$ locally computes DC_{ij} from its $Root_{ij}$ using the schedule tree T_i .
- 6: Execute Merge -Subcube (DC_i) to obtain the correct i-subcube DC_i .

7: END FOR

In the remainder of this section, we present further details for Step 3 (how the schedule tree T_i is built) and Step 6 (how locally generated *i*-subcubes are merged) of Algorithm 1. Step 4, the optimized data partitioning, which is the main contribution of this paper, will be discussed in the next section.

In Step 3, our parallel algorithm uses as a building block a standard sequential top-down data cube method such as Pipesort (Sarawagi, et.al., 1996). Such methods have in common that they consist of a two-phase approach. In the first phase, a *schedule tree T* is constructed which is a subgraph of the lattice and contains as nodes the identifiers of all views to be constructed. Recall that view v is a parent of a view v' if v can be created from v'. The schedule tree T identifies the sequence in which the views are to be constructed in the second phase. The main difference between the various top-down data cube methods is the schedule tree T that they build. For example, Pipesort starts with the lattice and assigns to every view identifier an estimate of the size of the respective view (Flajolet & Martin, 1985; Shukla, et.al., 1996). It then computes the cost of the aggregate operation associated with each edge of the lattice. The schedule tree T is then built by scanning the lattice level by level and computing for each two subsequent levels of nodes, and the edges between them,

a minimum cost bi-partite matching. We use Pipesort to compute the schedule tree T_i in Step 3 of Algorithm 1 if *all* 2^d views are to be computed. For building the *partial* data cube, i.e. a subset of the 2^d possible views, we use a modified schedule tree construction method presented in (Dehne, et.al. 2003).

We now discuss how locally generated i-subcubes are merged in Step 6. In Step 5 of Algorithm 1, each processor P_j locally computes DC_{ij} from its local $Root_{ij}$. For a view v of S_i , let v_j be the local view created by processor P_j . We need to merge, for each view v in S_i , the p different views v_j created on the p different processors P_j . Consider Algorithm 1 for i=1 and the 1-subcube shown in Figure 2. In Step 2 of Algorithm 1, $Root_0 = R$ is globally sorted by ABCD. In Step 5, each processor P_j computes locally the cube DC_{1j} from its data set $Root_{0j}$. Consider the views $ABCD_j$, ABC_j , AB_j , and A_j computed in Step 5. All these views are in the same sort order as the global sort order created in Step 2 because they are a prefix of ABCD. We shall refer to these views as the prefix views. The other views, ABD_j , AC_j , ACD_j and AD_j , are not a prefix of ABCD and are therefore in a sort order that is different from the global sort order. We shall refer to them as the prefix pref

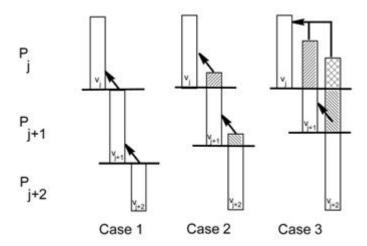


Figure 3: Illustration of cases for Merge- $Subcube(DC_i)$.

Consider a prefix view v and the problem of merging $v_1, ..., v_p$ stored on processors P_1 , ..., P_p . For example, consider the view v = AB in Figure 2 and the problem of merging AB_1 , ..., AB_p . The goal is to obtain a global AB sort order for $AB_1 \cup AB_2 ... \cup AB_p$ and then agglomerate those items that have the same values for dimensions A and B. Since AB is a prefix of the global sort order, ABCD, the first part is already done and the only items that, potentially, need to be agglomerated are the last item of v_i and the first item if v_{i+1} for each

 $1 \le j < p$. For each prefix view v every processor P_{j+1} simply sends the first item of v_{j+1} to processor P_j which compares it with the last item of v_j . Nothing else needs to be done in order to merge all v_j . Figure 3 illustrates the case of a prefix view v as "Case 1".

We now study the case of merging the views $v_1, ..., v_p$ stored on processors $P_1, ..., P_p$ for a non-prefix view v. For example, consider the view v=AC in Figure 2 and the problem of merging $AC_1, ..., AC_p$. Again, the goal is to obtain a global AC sort order for $AC_1 \cup AC_2 ... \cup AC_p$ and then agglomerate those items that have the same values for dimensions A and C. However, AC is not a prefix of ABCD and, therefore, the different v_j can have considerable overlap with respect to the AC order. Figure 3 illustrates the case of a non-prefix view v as "Case 2" and "Case 3". The rectangles represent the v_j with respect to AC order. The shaded areas represent the overlap which, in contrast to Case 1 (prefix view), can now be considerably more than just one element. We distinguish between a small overlap (Case 2) and large overlap (Case 3), depending on whether the overlap is smaller or larger than an experimentally chosen threshold value γ , respectively.

For each non-prefix view v, every processor P_j sends its first and last element to every other processor. Each processor P_k then determines its overlap with each P_j and sends that overlap to P_j . For each processor P_j let v'_j be the view v_j plus all the overlap received by processor P_j . We distinguish two cases which are both illustrated in Figure 3. The distinguishing criterion is the imbalance between the v'_j defined as $I(|v'_1|,|v'_2|, \ldots, |v'_p|) = \max\{(r_{max} - r_{avg})/r_{avg}, (r_{avg} - r_{min})/r_{avg}\}$, where r_{min}, r_{max} , and r_{avg} are the minimum, maximum and average of $\{|v'_1|,|v'_2|, \ldots, |v'_p|\}$, respectively. Case 2: IF $I(|v'_1|,|v'_2|, \ldots, |v'_p|) \le \gamma$ for a non-prefix view v THEN each P_j locally sorts v'_j and agglomerates the items with same values for dimensions in v. Case 3: IF $(|v'_1|,|v'_2|, \ldots, |v'_p|) > \gamma$ for a non-prefix view v THEN the v_j are merged by a global sort.

If the imbalance is smaller than γ (Case 2) then we proceed similar to Case 1. If the imbalance is larger than γ (Case 3) then we need to completely re-balance via a global sort. In fact, for Case 3 we do not wish to even route the overlap between processors. We rather re-sort immediately. Hence, in order to determine whether Case 2 or Case 3 applies, each processor P_k first determines the *size* of its overlap with each P_j and sends only the information about the size of that overlap to P_j .

A NEW OPTIMIZED DATA PARTITIONING METHOD

Good data partitioning is a key factor in obtaining good performance on shared nothing multiprocessors. Some researchers partition data on one or several dimensions (Goil & Choudhary, 1998; Muto & Kitsuregawa, 1999). They assume that the product of the cardinalities of these dimensions is much larger than the number of processors (Goil & Choudhary, 1998), in order to achieve sufficient parallelism. The advantage of their method is that they do not need to merge views across the network. For examples, if we partition on A, then ABC and AC do not need to be merged, or if we partition on A and B, then ABC and ABD do not need to be merged. However, in practice, this assumption is often not true. The cardinality of some dimensions may be small, such as gender, months and intervals for a numeric attribute. The number of processors in a parallel machine may be large, especially in clusters of workstations. Therefore, those methods are often not scalable. Our approach avoids these problems by partitioning on all dimensions and then applying a parallel merge procedure (Chen, et.al. 2004). The challenge here is that merge procedures based on fixed data partitioning schemes (Chen, et.al. 2004) often lead to excess inter-processor communications which may greatly reduce the speedup achieved by the parallel system and hence its effective scalability. In this paper, we improve on the results in (Chen, et.al. 2004) and present an optimized and dynamic data partition scheme for ROLAP data cube generation. This new dynamic data partitioning scheme adapts to both, the current data set and the performance parameters of the parallel machine. Our performance results show that our new partitioning scheme yields a significant performance and scalability improvement.

Our partitioning scheme adapts to the performance parameters of the parallel hardware. For a given parallel machine, we consider four performance parameters $t_{compute}$, t_{read} , t_{write} and $t_{network}$ defined as follows: $t_{compute}$ is the average time in microseconds to fetch/compare/store a data item in main memory; t_{read} is the average time in microseconds to read a data item from disk; t_{write} is the average time in microseconds to write a data item to disk; $t_{network}$ is the average time in microseconds for communicating a data item between processors. For heterogeneous parallel machines (e.g. clusters with different generations of processors), the parameters $t_{compute}$, t_{read} and t_{write} can differ between processors. In this case, we choose the parameters for the slowest processor. The parameter $t_{network}$ depends on both, the network hardware and the number of processors used. Based on the above four parameters, we devise a cost model to estimate the time for communication and computation, and determine the best data partitioning for Algorithm 1. Before starting

Algorithm 1, our software enters a test phase where it measures automatically the parameters $t_{compute}$, t_{read} , t_{write} and $t_{network}$ for the given machine.

After the i-th iteration of Step 2 of Algorithm 1, the j-partitions of $Root_i$ are well balanced over processors P_i ($1 \le j \le p$). However, as a result of the global sort, subsequent items with the same sort key may end up on two different (subsequent) processors. This is especially the case when the cardinality of some dimensions are small, such as for attributes like gender, months and intervals for a numeric attribute. The situation is illustrated in Figure 4 for an attribute "A" with attribute values a 1,a 2,...,a 10. When the data is sorted by "A" in Step 2, each processor receives a range of data as indicated. Consider the range of items with value a4. Some items are on Processor 1 and some are on Processor 2. The problem is that during the merging of subcubes in Step 6 of Algorithm 1, data movement occurs because Processor 2 has to send its items with value a4 to Processor 1. Instead, we could have made a4 the dividing line between the data between Processors 1 and 2 and moved all items with value a4 to Processor 2. We call this process "pivoting" and refer to a4 as the pivot. If we choose a4 as a pivot, then no data will have to be transferred between Processors 1 and 2 during the merging of subcubes in Step 6 of Algorithm 1. However, on the negative side, choosing a4 as a pivot introduces an imbalance in data size between Processors 1 and 2, and other steps of Algorithm 1 may now have a longer computation time because of this imbalance since the total computation time is always determined by the slowest processor.

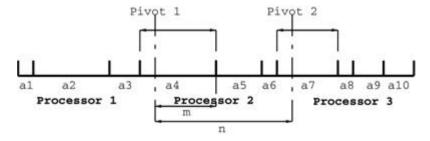


Figure 4: Data partitioning and *pivots*.

Our strategy is to choose pivots in such a way that we obtain the best tradeoff between lower communication due to less data movement and longer computation due to imbalance. We build a cost model to measure the impact of each possible pivot and choose the one with the lowest cost. We iterate this process until the total cost can be no further reduced.

We now present in detail our cost model and its impact on the performance of Algorithm 1 for a chosen set of pivots. We will later discuss how to select pivots. Note that Steps 2 and 3 are not impacted by pivots and, hence, our model measures only the performance of Step 4 (shifting partitions), Step 5 (computing cubes), and Step 6 (merging cubes).

An important factor to be taken into consideration is the impact of external memory. For our implementation of Algorithm 1, views that are small enough to fit into main memory are created in memory for better speed, while larger views are built in external memory through disk scan and external memory sort. In order to determine which version is used at run time, we define a maximal number of records, n_{max} . If the number of records of a view is smaller than n_{max} , we calculate the cost according to a formula for internal memory computation. Otherwise, we calculate the cost according to a formula for external memory computation. For example, if n_{max} is 1,000,000, view ABCD has 2,000,000 records and view ABC has 500,000 records, then we process ABC in main memory using the internal memory cost calculation and process ABC in external memory using the external memory cost calculation.

To calculate the cost of Steps 46 of Algorithm 1 for each view v, we use two basic numbers for each processor: n, the number of records stored at the processor and m, the number of moved records. Figure 4 illustrates n and m for Processor 2. The n and m values for $Root_i$ are obtained through a local linear scan. For every other view v in DC_i , we estimate values n_{est} and m_{est} as follows: Set n to the estimated view size calculated in Step 3 of Algorithm 1. Set $m = m_{Rooti} / n_{Rooti}$ where n_{Rooti} and m_{Rooti} are the n and m values for $Root_i$, respectively. Note that, a record is composed of d feature attributes and 1 measure attribute so that the size of a record is proportional to d+1.

We are now ready to analyze Steps 4 to 6 of Algorithm 1. For each step, we will give the cost for internal and external memory calculation and outline our rationale for the give n formulas.

Step 4. Scanning: $n(d/2) t_{compute}$ (internal memory), $n(d+1) t_{read} + n(d/2) t_{compute}$ (external memory). Exchanging: $m(d+1) t_{network}$ (internal memory), $m(d+1) t_{network}$ (external memory). Merging: $n(d/2) t_{compute}$ (internal memory), $n(d+1) t_{write} + n(d/2) t_{compute}$ (external memory). Rationale: Step 4 in Algorithm 1 shifts partitions of root views among processor. It consists of three sub-steps: scanning data, exchanging data and merging data. Each processor scans the local data and compares each row with the pivots considered. To compare a row with a pivot, we compare attribute values one by one. In the best case, only one comparison is needed, and d comparisons in the worst case, where d is the number of attributes. The average number of comparisons is d/2. In the external memory version, the cost for reading

data from disk is n(d+1) t_{read} , where n(d+1) is the number of items in $Root_i$ since each row contains d+1 items. In both versions, the communication cost is m(d+1) $t_{network}$, where m(d+1) is the number of items moved across the network. The cost of the last sub-step is n(d/2) $t_{compute}$. For the merging, the number of comparisons is a function of both, n and m. However m is much smaller than n and we ignore m in order to simplify calculations. In the external memory version, the cost for writing the data to disks is n(d+1) t_{write} . Note that, this is also an approximation since data is also exchanged between processors.

Step 5. Sorting: $n \log n \ t_{compute} + n(d/2) \ t_{compute}$ (internal memory), $n(d+1) \ t_{read} + n \log n \ t_{compute} + n(d/2) \ t_{compute}$ (external memory). Scanning: $n(d+1) \ t_{compute}$ (internal memory), $n(d+1) \ t_{write} + n(d+1) \ t_{compute}$ (external memory). Rationale: Step 5 of Algorithm 1 calculates the schedule tree used to generate the views. As described in (Sarawagi, et.al., 1996), we compute pipelines one by one. For each pipeline, the first view is sorted and the remaining views are generated by scanning. For example, in Figure 2, the schedule tree for the 1-subcube consists of a pipeline $ABCD \rightarrow BCD \rightarrow BC \rightarrow B$. The cost of sorting is $n \log n \ t_{compute} + n(d/2) \ t_{compute}$ (Dehne, et.al. 2003) for the internal memory version. The external memory version includes an additional cost for disk reading: $n(d+1) \ t_{read}$. The cost for scanning is $n(d/2) \ t_{compute}$ for the internal memory version, plus $n(d+1) \ t_{write}$ for the external memory version.

Step 6. Scanning: n(d/2) $t_{compute}$ (internal memory), n(d+1) $t_{read} + n(d/2)$ $t_{compute}$ (external memory). Exchanging: m(d+1) $t_{network}$ (internal memory), m(d+1) $t_{network}$ (external memory). Merging: n(d/2) $t_{compute}$ (internal memory), n(d+1) t_{write} + n(d/2) $t_{compute}$ (external memory). Rationale: Step 6 of Algorithm 1 merges i-subcubes between processors. The cost calculation is analogous to the calculation for Step 4.

Based on the above cost model, we evaluate possible partitionings and choose an optimal partitioning with minimum cost. Algorithm 2 shows our method to select a set of pivots and shift current partitions. The function Cost() represents the cost function for a given set of pivots as discussed above. Algorithm 2 first calculates the cost of the partitioning generated by Steps 2 and 3 of Algorithm 1 without any pivots. We then select pivots, calculate the cost based on those pivots and update the partitioning if the new cost is smaller than the old one. This process will continue until the cost can not be reduced any further. Unfortunately, the number of possible pivot combinations is very high. For p processors, the maximum number of possible pivots is p-1. Each pivot can either be not selected or selected for its left adjacent processor (all data move left) or selected for its right adjacent processor (all data move right). Therefore, the total number of possible data

partitionings is 3^{p-1} . If we have 32 processors in a cluster, the total number of partitionings is $3^{32-1} = 617,673,396,283,947$. In Algorithm 2, we choose a greedy method to reduce the cost as much as possible. In each iteration of the repeat-until loop we choose the pivot which generates the greatest cost reduction among all possible remaining pivots. We update the partitioning and the cost, and search again until we cannot reduce the cost further by adding another pivot. Algorithm 2 then re-partitions $Root_i$, using the chosen set of pivots.

Algorithm 2: Optimize - Partition($Root_i$)

- 1: Each processor P_j collects locally, for its data set $Root_{ij}$, the partitioning information (pivots and their n, m values) required for the evaluation of the function Cost(). The partitioning information is broadcast to all processors.
- 2: Each processor P_i computes cost = Cost (current partition without pivots).
- 3: done = FALSE.
- 4: REPEAT
- 5: **FOR** each processor P_i in parallel
- 6: Processor P_j calculates the new cost $cost_j^{new}$ obtained by adding pivot j, (moving the respective data to the left or right processor, whichever is lower cost).
- 7: **ENDFOR**
- 8: Let $cost^{new} = Min(cost_1^{new}, cost_2^{new}, ..., cost_{p-1}^{new})$
- 9: **IF** $cost^{new} < cost$
- 10: update partition by adding the chosen pivot.
- 11: cost=cost^{new}
- 12: **ELSE**
- 13: done = TRUE
- 14: **ENDIF**
- 15: UNTIL done
- 16: $Root_i$ is re-partitioned using the chosen set of pivots.

EXPERIMENTAL EVALUATION OF OUR NEW OPTIMIZED DATA PARTITIONING METHOD

In this Section, we analyze the performance gain obtained by our new optimized data partitioning method in comparison to (Chen, et.al. 2004).

We have implemented our optimized data partitioning method for shared-nothing data cube generation using C++ and the MPI communication library. This implementation evolved from (Chen, et.al. 2004), the code base for a fast sequential Pipesort (Dehne, et.al. 2002) and the sequential partial cube method described in (Dehne, et.al. 2003). Most of the required sequential graph algorithms, as well as data structures like hash tables and graph representations, were drawn from the LEDA library (LEDA, 2001).

Our experimental platform consists of a 32 node Beowulf style cluster with 16 nodes based on 2.0 GHz Intel Xeon processors and 16 more nodes based on 17 GHz Intel Xeon processors. Each node was equipped with 1 GB RAM, two 40GB 7200 RPM IDE disk drives and an onboard Inter Pro 1000 XT NIC. Each node was running Linux Redhat 7.2 with gcc 2.95.3 and MPI/LAM 6.5.6. as part of a ROCKS cluster distribution. All nodes were interconnected via a Cisco 6509 GigE switch.

Our implementation of Algorithm 1 initially runs a performance test to calculate the key machine specific cost parameters, $t_{compute}$, t_{read} , t_{write} and $t_{network}$, that drive our optimized dynamic data partitioning method. On our experimental platform these parameters were as follows: $t_{compute}$ =0.0293 microseconds, t_{read} = 0.0072 microseconds, t_{write} =0.2730 microseconds. The network parameter, $t_{network}$, captures the performance characteristics of the MPI operation "MPI_ALL_TO_ALL_v" on a fixed amount of data relative to the number of processors involved in the communication. On our experimental platform, $t_{network}$ = 0.0551, 0.0873, 0.1592, 0.2553, 0.4537, and 0.5445 microseconds for p = 2, 4, 8, 16, 24, and 32, respectively.

In our experiments all sequential times were measured as wall clock times in seconds. All parallel times were measured as the wall clock time between the start of the first process and the termination of the last process. We will refer to the latter as *parallel wall clock time*. All times include the time taken to read the input from files and write the output into files. Furthermore, all wall clock times were measured with no other users on the machine.

Figure 5 shows for full cube construction the parallel wall clock time observed for data sets of N=8 million records, with and without optimized data partitioning, as a function of the number of processors used. Figure 6 shows the corresponding relative S_p for p

processors defined as $S_p = t_1 / t_p$, where t_1 is the running time of the parallel program using one processor (all communication overhead having been removed from the program) and t_p is the running time using p processors.

The main observation is that optimized data partitioning leads to a significant improvement in speedup and scalability. Without our new optimization method, relative speedup hovers around 50% of optimal. With our new optimization method, we obtain linear (i.e. optimal) relative speedup for as many as 30 processors. This is an impressive improvement in speedup and scalability.

Throughout these experiments, as we increased the number of processors we observed two countervailing trends. Increasing processors, while holding total data size constant, leads to less data per processor and therefore better relative speedup because each processor can fit more of its data in memory, thereby reducing disk related overheads. On the other hand, using standard GigE switches and a standard MPI implementation, increasing the number of processors reduces the speed of communication, even when total data size communicated is held constant, and therefore tends to reduce relative speedup. The slight super linear effects observed for example at 16 processors in Figure 6 result when the benefits of fitting data in memory outweigh the penalties associated with higher communication overheads.

Figure 7 shows for full cube construction with optimized partitioning the parallel wall clock time in seconds on a p=32 node cluster as a function of the data size N=16M, 32M, 48M, 64M, 128M, and 256M records. We observe that, with optimized partitioning, when we double the input size of the cube being generated at most twice the time is required. This holds true even for extremely large cubes where the input consists of 256 million rows of data (9.2 Gigabytes) and the output consists of a data cube consisting of 2^d views containing a total of ≈ 7 billion rows (200 Gigabytes), despite the fact that we are not scaling network bandwidth, in large part because of the improved data balance.

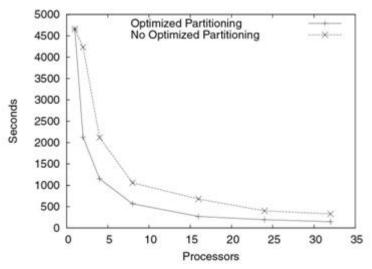


Figure 5: Parallel wall clock time in seconds as a function of the number of processors with and without optimized data partitioning.

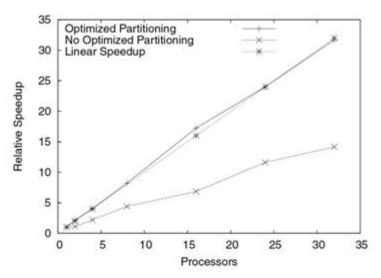


Figure 6: Relative speedup corresponding to Figure 5.

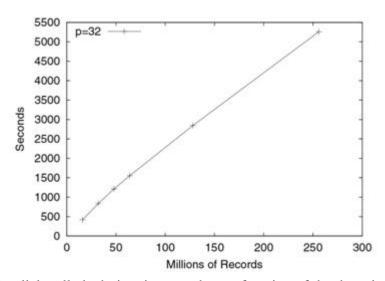


Figure 7: Parallel wall clock time in seconds as a function of the data size N = 16M, 32M, 48M, 64M, 128M, and 256M records.

IN DEPTH TESTING OF OUR NEW PARALLEL DATA CUBE COSTRUCTION METHOD

In this section, we report in more detail on how our new parallel data cube construction method performed under various loads and conditions in order to further illuminate its strengths and weaknesses.

For this series of experiments we generated a large number of synthetic data sets which varied in terms of the following parameters: N - number of records, d - number of dimensions, $|D_1|$, $|D_2|$, ..., $|D_d|$ - cardinality in each dimension, and a_1 , a_2 , ..., a_d - skew in each dimension. Unless otherwise stated, the following defaults were used for these parameters: dimensions d = 8, cardinalities $|D_i| = 256$, 128, 64, 32, 16, 8, 4, 2, skew $\alpha = 0$ in all dimensions, and percentage of views selected k = 100%.

Relative Speedup

Speedup is one of key metrics for evaluation of parallel database systems (DeWitt & Gray, 1992) as it indicates the degree to which adding processors decreases the running time. Figure 8 shows for full cube construction the parallel wall clock time observed for data sets of varying sizes as a function of the number of processors used, and Figure 9 shows the

corresponding relative speedup. As is typically the case, relative speedup improves as we increase the size of the input and hence the total amount of work to be performed. For N = 8,000,000 records, optimal linear relative speedup can be observed all the way up to 32 processors, while for fewer N = 1,000,000 records speedup drops off beyond 4 processors. In general, linear speedup is observed when there are at least N/p = 250,000 records per processor.

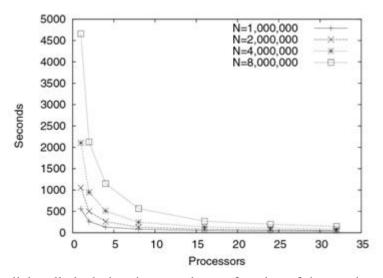


Figure 8: Parallel wall clock time in seconds as a function of the number of processors for data of size N = 1M, 2M, 4M and 8M records.

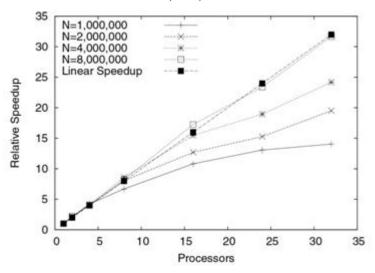


Figure 9: Relative speedup corresponding to Figure 8.

Partial Cubes

In many applications, users do not require all of the 2^d views contained in a full data cube but rather only a selected subset. The challenge for a partial cube generation method is to efficiently construct the set of selected views, maintaining relative efficiency even as the number of views (and therefore total work) is decreased. Figure 10 shows for *partial* cube construction the parallel wall clock time observed for a range of different percentages of selected views as a function of the number of processors, and shows Figure 11 the corresponding relative speedup. Note that near optimal speedup is achieved for a range of different percentages of selected views up to 16 processors. Beyond that there is a reduction in speedup for smaller sets of selected views, in large part because there is simply not enough work to keep all of the processors busy.

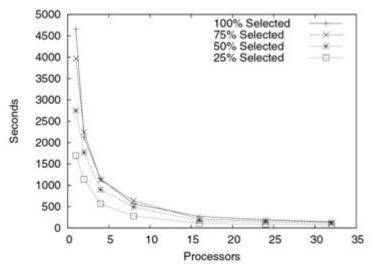


Figure 10: Parallel wall clock time in seconds as a function of the number of processors for partial cubes with percentage of selected views k = 100%, 75%, 50%, and 25%.

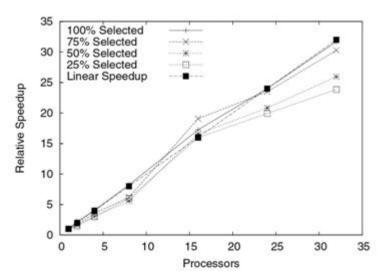


Figure 11: Relative speedup corresponding to Figure 10.

Scaleup

Scaleup is another key metric for the evaluation of parallel database systems (DeWitt & Gray, 1992). It indicates whether a constant running time can be maintained as the workbad is increased by adding a proportional numbers of processors and disks. Figure 12 shows for full cube construction the parallel wall clock time observed as a function of the number of processors used when N/p=0.125M, 0.25M, 0.5M, and 1M records per processor. Overall, we observe good scaleup. Initially, when we double the number of processors and double the size of the input, we observe a better than linear scaleup for all curves in Figure 12. This is due to the fact that we are keeping the cardinalities of attributes constant as we increase the data size and therefore the relative density of the data cube is increasing, which is beneficial for top-down generation methods (Agarwal, et.al. 1996; Sarawagi, et.al., 1996). This increase in relative density leads to more agglomeration and therefore a smaller output data size per processor, as illustrated in Figure 13. However, this effect is offset by the fact that the network bandwidth is not being scaled as we increase the total input size N. As we increase the data size per processor, more data has to be moved across the network as can be seen in Figure 13. When the total input size N is greater than 8M records, network congestion on our switch begins to degrade the scaleup performance. However this effect can be observed to flatten out after N reaches 16M records.

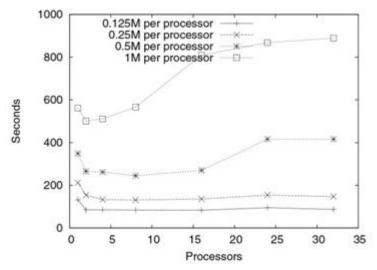


Figure 12: Scaleup for data size of N/p = 1M, 0.5M, 0.25M and 0.125M records per processor.

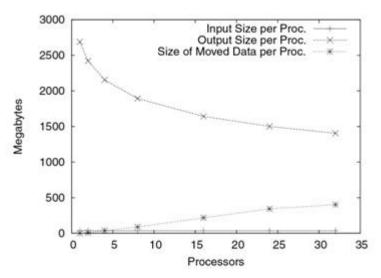


Figure 13: Output sizes per processor for input of N/p = 1M records per processor.

Sizeup

Sizeup is similar to scaleup but considers the number of processors fixed It indicates whether a proportional running time can be maintained as the workload is increased. The sizeup for x units of workload is defined as $U_x = \frac{t_x}{t_1}$, where t_1 is the running time of one unit workload and t_x is the running time of x unit workload. An ideal U_x is x, which implies that x units of workload costs x times more time than one unit of workload. Hence, the curve for

ideal sizeup is a linear diagonal. Figure 14 shows for full cube construction the sizeup observed for data sets between 1 and 8 million records using between 1 and 32 processors. We observe that the sizeup curves are all approximately linear. The actual slope of the curves is determined by the percentage of the parallel overhead for fixed p when N = 1,000,000. Figure 15 shows for full cube construction the relative sizeup observed for data sets between 1 and 256 million records on p=32 processors. Even with these large data sets we observe good sizeup performance.

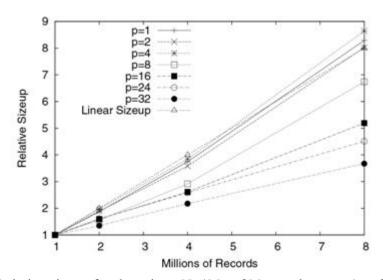


Figure 14: Relative sizeup for data sizes N=1M to 8M records on p=1 to 32 processors.

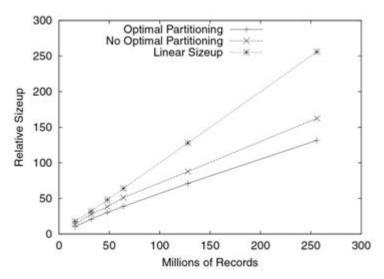


Figure 15: Relative sizeup for p=32 and input data of size N=16M, 32M, 48M, 64M, 128M, and 256M records. Corresponds to Figure 7.

Data Skew

Data sets with skewed distributions can pose an interesting challenge to parallel data cube generation methods. As skew increases, data reduction tends to increase, particularly in top-down generation methods (Agarwal, et.al. 1996; Sarawagi, et.al., 1996). Data reduction is typically positive, as it reduces the total amount of work to be performed. However, if data reduction is large and unevenly spread across the processors it may unbalance the parallel computation and cause the amount of data that has to be communicated to rise sharply. To explore this issue we generated data sets using the standard ZIPF (Zipf, 1949) distribution in each dimension with α =0 (no skew) to α =2 (high skew). Figure 16 shows for cube construction the parallel wall clock time observed as a function of the skew for α =0,1,2, and Figure 17 the corresponding relative speedup. We observe that, in general, as skew is increased parallel time decreases due to data reduction and decreased local computation. Our data partitioning optimization appears to handle gracefully the resulting data imbalance by shifting data appropriately. However, if this data reduction is very large, as for α =2, it reduces the opportunities for speedup as there is simply much less work to be parallelized.

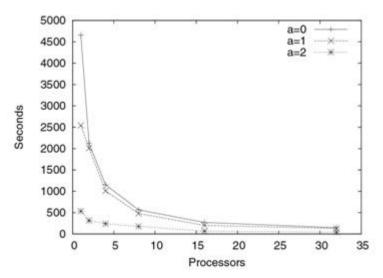


Figure 16: Parallel wall clock time in seconds as a function of the skew for α =0,1,2.

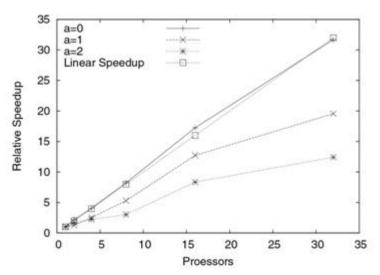
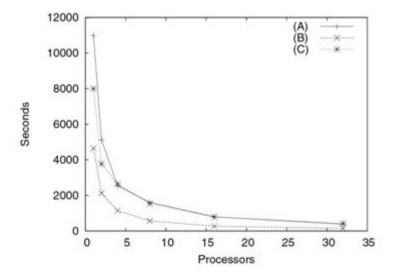


Figure 17: Relative speedup corresponding to Figure 16.

Cardinalities of Dimensions

The cardinalities of the different dimensions in a data set can affect the performance of our algorithm. As cardinalities increase so does the sparsity of the data set and this may adversely effect parallel time especially given that top-down methods (Agarwal, et.al. 1996; Sarawagi, et.al., 1996) are designed primarily for dense data cubes. Curves A, B and C of Figure 18 clearly illustrate this effect. The sparser data sets require significantly more time, although, as can be seen in Figure 19, this has a positive effect on the relative speedup achieved.



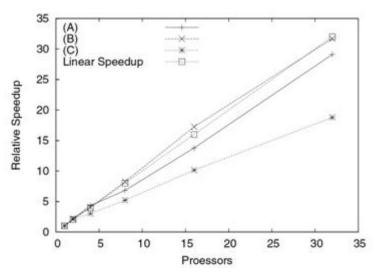


Figure 19: Relative speedup corresponding to Figure 18.

CONCLUSION

In this paper, we present an optimized data partitioning method for parallel ROLAP data cube construction on shared-nothing multiprocessors that can provide a *significant* performance improvement. Our optimized data partitioning method adapts to both, the current data set and the performance parameters of the machine. In comparison with previous approaches, our new method has a significantly better *scalability* with respect to the number of processors. Optimal speedup for as many as 32 processors was not observed for previous parallel methods (Chen, et.al. 2004; Dehne, et.al. 2001; Dehne, et.al. 2002; Goil & Choudhary, 1997; Goil & Choudhary, 1999; Lu, et.al., 1997; Muto & Kitsuregawa, 1999; Ng, et.al., 2001). In addition, because of its shared nothing approach, our new method does also significantly improve the scalability with respect to the I/O bandwidth (number of parallel disks) which is of great importance for handling large data sets.

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